## Examination of Water Production and Sewage Flow Forecasting at the Washington Suburban Sanitary Commission and Recommendations for Improvements

FINAL REPORT

by

Roland C. Steiner and Daniel P. Sheer

November 1985

CO-OP Section
Interstate Commission on the Potomac River Basin
6110 Executive Boulevard, Suite 300
Rockville, Maryland 20852

(301) 984-1908

#### Acknowledgement

The help and advice of Mr. Nicholas J. Del Grosso, of the WSSC Water Resources Planning Section is much appreciated. His cooperation in the provision of data, information, and examples of forecasting methods at the WSSC was particularly helpful during the course of this study. Other WSSC staff who provided information on specific topics include Thomas E. Gingrich, John W. DiLoreto, Thomas M. Fischer, William Austin, and Marjorie L. Johnson.

In addition, Nazir Baig and Dominic J. Motta, among others, of the Montgomery and Prince George's County offices respectively, of the Maryland-National Capital Park and Planning Commission made documents available for reference and provided interpretation of population, housing and employment forecasts.

#### SUMMARY

Based on our examination of water production and sewage flow forecasting at the Washington Suburban Sanitary Commission, we offer a summary of our conclusions in the form of an evaluation of present methods and recommendations for improvement.

#### Evaluation:

- 1. In general, the methods used to forecast water production and sewage flow are consistent with the best contemporary practice in the water supply industry.
- 2. Data and information are organized and synthesized carefully in order to provide historical perspective and credible data bases. This is evidenced in the <u>Distribution System Storage Study</u>, The Development of Sewage Flow Factors and Their use in <u>Forecasting Sewage Flow</u>, and <u>Residential Flow Factor Analysis</u>.
- 3. In general, forecasting at WSSC involves the development of disaggregated demand factors (coefficients) on moderately large and relatively homogeneous customer groups. These factors are derived from recently initiated accounts in order to best reflect the type of customers who will be the constituents of future growth. Continuing use of the extensive computerized data processing facilities contributes to the good quality of forecasting methods.
- 4. The factors are applied to forecasts of future customer groups which are produced by an independent specialized cooperative process (the Cooperative Forecasting Program) designed to obtain the best results. This technique is superior to simply projecting past trends in water production and sewage flows.
- 5. Generally, although not always, forecasts are well documented with sources of data and explanations of methods.
- 6. In a comparison with the local electric utilities (which produce a commodity whose demand is driven by factors which are similar in many respects to those of water and sewer services) the forecasting practices at WSSC are similar in detail and extent.

#### Recommendations:

A number of inconsistencies and areas for improvement were detected during the course of the study. Their reconciliation and incorporation would enhance the forecasting process at WSSC.

- 1. Use of the Commission's <u>Design Manual</u> is rendered somewhat confusing and ambiguous due to the lack of documentation of the factors contained in the Appendices. There ought to be an accompanying explanation of how and when the factors were derived. Further, there should be differentiation between water production and sewage flow factors in order to take account of water main transmission losses, inflow/infiltration, and other distinguishing characteristics; and geographic disaggregation should be provided if appropriate.
- 2. The effects of changes in price and income should be incorporated into the forecasting process. Although the debate over the price elasticity of demand for water is far from finished, enough evidence is available to suggest that economics is a significant influence. Some degree of coordination with those involved in the preparation of the WSSC budget should be established.
- 3. A pattern of frequent re-evaluation of factors and their application should be adopted. In particular, Chapter IV of the <u>Distribution System Storage Study, Project 6.02</u>, should be updated and expanded for use in forecasting for planning purposes.
- 4. The value of increased disaggregation by property code, service type and location as available from billing records should be investigated. If significant differences exist among the many groups of customers, they should be further segregated for analysis and forecasting.
- 5. The currently available Round III Cooperative Forecasts of housing and employment should be used to update the analysis presented in the <u>Water Production Report Through June, 1982</u>. In the process of updating, this report might effectively be combined with <u>Distribution System Storage Study, Project 6.02</u>, in order to reduce duplication of effort and reference material.
- 6. The use of probability in the field of forecasting and control is now well established and should be incorporated into the forecasts produced by the Commission. Perhaps the simplest and most useful applications would be in presenting confidence limits on forecasts, and expressing results in the format of probabilities of exceedence.

7. A small, but significant recommendation, is to revise the results in the report <u>Flow Projections for Workload Indices</u>. The forecast should have as its base level the value of the normalized data regression line for FY'84, not the normalized value of flow for that year. Water use data for the analysis in this report have recently been changed to reflect water "consumption" only, excluding usage through submeters which is not returned to the sewers. These data are more representative figures for sewage flow calculations than total water "production". The derivation of work indices for water should be fully documented.

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#### Introduction

This report presents the results of an external examination of WSSC techniques used by staff of the WSSC in the development of forecasts of water production and sewage flow. The analysis focuses on the use of available data and information, and the degree to which that use is consistent with good and contemporary forecasting practice. The motivation for an external examination came from inconsistencies in the approach to forecasting methodology between WSSC staff and one or more of the Commissioners.

The organization of the report follows the format of addressing the nine inter-related tasks as set out in the proposal:

- 1. summarization and use of presently available data and information at WSSC, County Planning Boards of the Maryland-National Capital Park and Planning Commission, and Metropolitan Washington Council of Governments,
- 2. analysis of unit production and flow factors with respect to WSSC property codes, service types, and counties,
- 3. analysis of the effects of change in price and income levels,
- 4. investigation and incorporation of uncertainty due to weather into flow forecasting techniques,
- 5. incorporation of alternate future population, housing unit and employment scenarios into forecasts,
- 6. presentation of individual forecasts which are conditional upon discrete assumptions about the future,
- 7. presentation of example probabilistic forecasts in terms of probabilities of exceedence,
- 8. ex-post examination of previous plans and forecasts at the WSSC and planning agencies in order to determine historical accuracy, bias and variance,
- 9. outline future directions in data availability, analytical tools, forecasting techniques, and planning applications.

An Appendix, which contains a photocopy of an example of monthly climatological data, follows the main body of the report.

#### Forecasting Defined

Forecasting can be defined as both an objective and a subjective process: it is the subjective application of objective material. A forecast is a statement about the future which is conditioned on objective or factually derived relationships and influenced by various assumptions. It is subjective in that it is a statement about the future and therefore cannot be factual, but speculative.

Good and contemporary practice of forecasting involves the bringing together and analysis of all the pertinent information that time and effort will allow in the competition for limited resources, and having regard for the use to which the forecasts will be put and its relative costs and benefits. The information should be the most up-to-date that is available, but should be regarded in the context of previous information, and subject to change as new and revised information becomes available. The process of forecasting usually includes the establishment of a base level from which the forecast begins, and an examination of previous conditions in order to establish trends. Information which could influence the continuance of established trends is brought into the forecasting process so that final results are not a blind projection of the past.

#### Report of Work

All of the analyses, computations and results developed in this study make use of the latest available planning and forecast data which are relevant to the Washington Suburban Sanitary District (WSSD). The execution of the study is described in the fulfillment of nine interconnected tasks.

#### TASK 1

Evaluate the available data and information relative to forecasting the demand for water and sewer services in the WSSD.

The evaluation has concentrated on material which would be of most use in medium to long term forecasts for purposes of planning raw water and distribution facilities, sewage collection and treatment facilities, and budget considerations in the out years. The data and information is derived from reports and other documentary material, and from personal contact with persons involved with the collection of such data or the forecasting of future values. The material must necessarily cover past conditions of water production, sewer flow and explanatory variables, as well as forecasts of those explanatory variables and their functional relationships with respect to water and sewage.

The pursuit and analysis of information may sometimes be frustrating and tedious, and inevitably some overlap of information will be encountered in the descriptive and interpretive reference material. The organization and synthesis of data is certainly an important aspect of producing credible forecasts, and should be undertaken carefully.

There follows a summary of data and information available for forecasting the demand for water and sewer services in the WSSD. This information is organized by the providing agency.

#### WSSC

Documentary material including:

#### WSSC <u>Design Manual</u>

The Commission follows the practice of maintaining a <u>Design Manual</u>. Relevant information to forecasting for planning purposes is contained in several of the Appendices. Appendix D contains Flow Factors (coefficients) for numerous types of water using

property, including types of housing, and educational institutions, retail and commercial properties. There is, however, no areal differentiation and no documentation refering to the method or date of derivation of these Factors. The lack of explanation fosters skepticism of their value as forecasting aids and contributes to the fact that they may not be regarded or used as well as they might be. Appendices E and F contain Dwelling and Acreage Factors respectively for the various land use zoning classifications, differentiated by County. Again, there is no supporting information as to date or method of derivation.

#### Special Studies:

ADC Trends

The Office of the Secretary of the Commission has conducted a series of studies which examine the consumption behavior of customers by Average Daily Consumption (ADC) group. The results of these studies are of use in understanding the relationship of water use to price, and in particular in seeing the effect of the Conservation Orientated Rate Structure which was introduced January 1, 1978. Although there is considerable unresolved debate as to the price elasticity of demand for water and sewer services, more of this kind of information on the effects of changes in rates, personal income and general rates of inflation should be incorporated in the forecasting process. No allowance for variations in weather seems to have been incorporated in this work.

Inter-office and inter-agency correspondence
A considerable body of data and information relative to
forecasting exists in the files of the Water Resources
Planning Section. Much of the best described and
documented work is contained in the following reports:

- Distribution System Storage Study
   Project 6.02
   Water System Planning Section, June, 1980.
- 2. The Development of Sewage Flow Factors and Their use in Forecasting Sewage Flow by Edward Graham Sewer System Planning Section, November, 1981
- 3. Residential Flow Factor Analysis
  Contract No. 83MM1093-A
  by Nick Del Grosso and Bruce Downes
  Planning and Engineering Division, November,
  1984

These reports provide excellent background material and should be referred to in all forecasting exercises. It is recommended that the material in Chapter IV, on water demands, of the <u>Distribution System Storage</u> Study, Project 6.02, be updated and expanded for use in forecasting for planning purposes.

#### Flow Book

The Flow Book, being a compilation of computer generated data reports, is an important and consistent source of basic data necessary in the preparation of forecasts. Particularly useful reports in the Flow Book generally contain monthly data back through 1977 for average and rolling annual average sewage flows to each sewage treatment plant, monthly total precipitation at three area rain gauges, and monthly water produced at the Potomac and Patuxent treatment These data (together with monthly temperatures available from the National Weather Service, Ref: NOAA and the Appendix) would be useful in expanding the Commission's efforts in normalizing water demand and sewer flows for varying weather conditions so as to more accurately understand the response to growth in housing and employment.

#### Plumbing Code

The regulations governing the installation and water using characteristics of new and replacement plumbing fixtures in the WSSD reflect the evolution of water conservation. The limitations on water use have successively decreased the permissible amount of flow through fixtures, and have progressively applied to more and more types of fixtures as summarized in Table 1. This information, together with some estimate of fixture usage, might provide a quantitative factor for incorporation into the forecasting process.

#### TABLE 1 Conservation Plumbing Code

Regulations Governing the Installation of Plumbing and Sewer Cleaning in the Washington Suburban Sanitary District

Issue Date 1961 1965 1972 1976 1980 1983 1984

Quantity (gal) or Flow (gpm)

Flushometer [gal]		(	
Toilet	>5	>3.5 <3.5	5
Urinal		<3.0	
Toilet (tank) [gal]		<3.5	
Shower (stall) [qpm]		<3.5	<3.0
Sink Faucets (h+c) [gpm]			<4.0
Lavatories (h+c) [qpm]			<4.0
(hot only) [gpm]			<0.25

#### Historical Perspective

In the preparation of all forecasts, an examination should be made of the accuracy and assumptions employed in previous efforts. This would give an historical context and perspective that would aid in the accuracy, understanding and interpretation of the forecast. The reports mentioned above contain significant elements of historical documentation.

#### Personal Consultation:

The interpretation of documentary material, on whatever subject, is always enhanced by personal contact with staff involved in the production or use of that material. Among others, helpful resource people contacted for data and information in this study are

listed below. It is important to realize that with employment turnover and organizational changes, individual personnel may come and go, but the institutional structure should be such that the data and information is maintained in a consistent and available manner.

Nicholas J. Del Grosso of the Water Resources Planning Section is helpful in matters relating to sewage flows.

Thomas E. Gingrich
of the Water Resources Planning Section is helpful
in matters relating to water production.

John W. DiLoreto is helpful in matters relating to the plumbing code.

Thomas M. Fischer of the Secretary's Office is helpful in matters relating to changes in consumption over time.

William Austin is helpful in matters relating to water and sewer billing.

Marjorie L. Johnson
of the Public Affairs Office is helpful in matters
relating to water conservation programs.

Montgomery County Planning Board of the Maryland-National Capital Park and Planning Commission

Documentary material including:

Comprehensive Planning Policies Report (annual)

This report contains a combined set of interrelated policies and data in one convenient reference volume. It also contains updated inventory data on development progress for County population and housing, and extracts of all previously adopted staging policies as contained in various master plans, sector plans and functional plans. The housing unit development status information is among the most important in this document. High, intermediate and low forecasts are compared with actual growth data. The latest population and employment forecasts are also given by Policy and Planning areas.

#### Long Range Forecast; People, Jobs and Housing

This publication, dated August 1979, presents a long range projection and analysis of population, households and employment growth to the year 2000 in Montgomery County and the Washington Region. It presents a more detailed Ten Year Forecast for Montgomery County. These forecasts are based on the Metropolitan Washington Council of Governments' (COG) Cooperative Forecasting Program. Round II and Round I Forecasts are compared; and high, low, and intermediate forecasts are given and defined. The high alternative is the greatest amount of growth which is foreseen to occur, whereas the low alternative is the minimum growth The intermediate forecast foreseen to occur. represents the County's attempt to forecast a most likely level of growth given the information available at the time the forecasts were developed. probabilities of occurrence are associated with either of the extreme forecasts, but they are produced as an acknowledgement of the uncertainty inherent in forecasting and as a possible tool for use in risk assessment.

#### County Comprehensive Water and Sewer Plans

Under State law (Section 9-505, Health-Environmental Article), each county must adopt a plan that provides for the orderly expansion and extension of systems dealing with sewage, water supply, and solid waste disposal for at least a 10-year period. These plans are subject to review and approval by the State Department of Health and Mental Hygiene and are subject to periodic amendment or revision. The plans include:

- present level of use and existing capacity for each sewage treatment drainage basin or service area,
- population projections, anticipated treatment needs, and planned facilities,
- 3. water supply and waste disposal needs and planned facilities.

The population, housing and employment data and forecasts, as presented in these plans in recent years, have been drawn from the COG Cooperative Forecasting Program. They are based on county policy and planning areas, and extend by 5-year increments to the year 2000. In addition, current and future estimates of population (including ultimate capacity values) are given for major drainage basins in the county. This is of direct benefit in planning for sewer facilities. Recent plans have also tried to address the variability

recognized in several of the influential factors affecting sewage flow. These include: growth rate forecasts, infiltration/inflow, water consumption, facility capacity rating, commitment policy and septic relief. Each factor and its possible effects are Household size (given in the 10-year plans) discussed. is an important factor used in converting from population estimates to numbers of housing units and then to water demand or sewer flow. Although much of the water and sewer data contained in the 10-year plans are doubtless supplied by WSSC, there is much to be gleaned in a qualitative sense for forecasting from the development and employment policies presented by the counties in those documents. An important function of the plans has been to attempt to define the "holding capacity" of the land; or in other words, its ultimate carrying capacity for development under present and future foreseen zoning limitations. This information is of great benefit to the WSSC for the planning of water and sewer facilities in that it helps define the present position in relation to the ultimate maximum potential demand for water and sewer services. Redevelopment, changes in the technology of water use and sewage generation, and other factors which continue to affect demand at full land use development must still be considered.

#### Personal Consultation

As stated in the Personal Consultation section under WSSC above, direct contact with relevant staff is helpful in complementing and interpreting published information. Those at Montgomery County included:

Nazir Baiq

Environmental Planning Coordinator.

#### Robert Hnat

is helpful in matters concerning forecasts of dwelling units and holding capacity of the land in Montgomery County.

Prince George's County Planning Department, Maryland-National Capital Park and Planning Commission

Documentary material including:

#### Growth Trends in Prince George's County and the Region: 1950-2000

This report, published by the Research and Special Studies Division in November 1979, presents the growth and development trends expected to occur in Prince George's County from the mid-1970's to the year 2000. A good summary of growth from 1950 puts the future projections in perspective, and the County is viewed in the context of the entire Washington Metropolitan Area. The report focuses on the amount of growth that is likely to occur in population, households and employment. Projections are based on the then-current forecasts for the metropolitan area (Round II) and include descriptions of the basic process, methodology and assumptions. The report is concise, yet full of clearly stated detailed information and useful data, including: employment by industrial sector, average household size, dwelling unit completions, and a statement of assumptions used to produce low, intermediate and high future development scenarios. addition, comparisons are made with previous forecasts of population and employment.

### Estimates and Forecasts of Dwelling Units, Population and Employment in Prince George's County This report, published in July 1981, presents useful

This report, published in July 1981, presents useful information on the following subjects: assumptions used for dwelling unit and population forecasts 1980-2000; low, intermediate, and high alternative development scenarios; small area population forecast methodology; low, intermediate, and high alternative employment scenario assumptions; population/employment ratios; and employment forecasts by industrial sector. The degree of documentation of data and assumptions in this report contribute to making it a useful reference for water and sewer service demand forecasting.

#### Forecasts of Growth in Prince George's County, Maryland: 1980-2010

This document is sub-titled "Results of the Round III Cooperative Forecasting Program" and published in March 1984. It contains results of the most sophisticated analysis and assumptions to date, and is proportionately useful in preparing forecasts of future

water and sewer use. Significant features include: geographic disaggregation by Policy Analysis Zone; 5-year interval forecasts to 2010; high, intermediate, and low development scenarios; household size projections; dwelling unit projections by single family and multi-family type; population projections by households and group quarters; and employment projections by industry group.

County Comprehensive Water and Sewer Plans

The Prince George's County 10-year Comprehensive Water and Sewer Plans provide substantially the same data and information with respect to development in this county as do the 10-year plans for Montgomery County, as previously described. This data includes estimates and forecasts of single and multifamily dwelling units, the COG intermediate population and employment values geographically disaggregated by sewer service areas.

Personal Consultation

Direct contact with the following personnel proved helpful with the interpretation of reference material:

Dominic J. Motta

of the Environmental Planning Division is knowledgable concerning 10-year Water and Sewer Plans.

Joseph Valenza

is helpful with the comparison of successive planning and forecasting efforts.

Metropolitan Washington Council of Governments

Documentary material including:

Cooperative Forecasting, Round III Technical Report - 1984

Data and information presented in this report form the basis of local and regional forecasts in the Washington Metropolitan Area. It contains forecasts of population, households and employment which are developed through a cooperative process involving the Council of Governments (COG), its member jurisdictions, the states, and other planning agencies. This cooperative process is the best effort at producing local and regional forecasts which are coordinated in order to minimize local distortions. The report documents the forecasting process and

presents results for the period 1980-2010. In addition to local and regional forecasts, a geographic disaggregation is made on the basis of COG Analysis Districts. This is perhaps the most important and current document to be consulted when conducting forecasts for water and sewer services. As time passes, local jurisdictions may update their forecasts prior to the succeeding Round of Cooperative Forecasts.

Cooperative Forecasting, Round III Summary Report - 1984
This document presents the principal elements of the Round III Technical Report described above.

#### Personal Consultation John McLean

confirmed that the Round III Technical Report contained a full comparison with previous Rounds.

#### Miscellaneous

#### Wolman reports

Early reports of consultants chaired by Abel Wolman on future sewerage requirements for the area present forecasts with factors of 100 gpcd, and 200 gal/acre/day infiltration; and commercial, industrial and institutional acreage with specified design gal/acre/day factors. Population projections, including ultimate capacity values, and forecasts of waste water flows are given for ten year intervals from 1960 to 2000.

#### Bi-County Water Supply Study

Considers existing demand for water and anticipated future demand. The report covers the subjects of future shortages, restrictions and structural solutions, although very little documentation of forecast assumptions is provided.

Other reports of studies involving demand forecasts for water and/or sewer services do exist. These include the Northeastern United States Water Supply Study and the Metropolitan Washington Area Water Supply Study, both by the U.S. Army Corps of Engineers.

Good forecasting practice involves the use of as much relevant data and information as time will permit, and subject to the intended application of the forecast. In partial fulfillment of this objective, demand forecasting techniques at the electric

utilities in the Washington area were examined. The demands for gas and electric services have many similarities to those for water and sewer services. Therefore, an inquiry into the way in which that industry produces its forecasts of demand might uncover useful applications for water and sewage forecasting.

Baltimore Gas & Electric Company

Mr. Ernest Dawson, General Supervisor for Forecasting, provided the following information. Demand forecasting is performed on disaggregate customer groups: residential, commercial and industrial. The residential group is further disaggregated by similar types, and future estimates of housing starts and recent completions also factor into forecasts of demand. In addition, engineering models (those that rely on appliance censuses, usage and saturation rates) are applied to residential use forecasting. Commercial and industrial sector demand forecasts are functions of employment and industrial production. There is also some consideration of geographical distribution of demand, and the effects of price and income are analyzed. Sources of data for explanatory variables include: Chase Econometrics for industrial production indicies, employment, and personal income; the Regional Planning Council for demographic data; BG&E accounts for customer types and usage; and BG&E marketing surveys for residential appliance and industrial utilization information.

#### Potomac Electric Power Company

Mr. Edward Mayberry, Manager of the Forecasting Division, provided the following information. Electricity demand forecasting is carried out on several time scales; from hourly to long-term. Auto-regressive moving average (ARMA) models with transfer functions are developed and employed. Weather parameters drive demand: cooling degree days, humidity, etc. Other influential factors taken into account in modeling include: employment, price of product, price of household appliances. There is extensive customer disaggregation by major types of use (electric space heating, water heating, air conditioning) for all customers, and further commercial and industrial groups are based on size and pattern of demand. In addition, some geographic disaggregation is performed. Relatively sophisticated sensitivity analysis is performed with Monte Carlo simulation techniques in order to derive a probabilistic range of forecasts. Sources of data for explanatory variables include: Chase Econometrics for long-term macro economic forecasts; Bureau of Labor Statistics, Bureau of Census, Commerce Department (in general) for historic data. Based on these data Pepco has developed its own models for forecasting employment and demographic information.

WSSC planning staff develop disaggregated demand factors (coefficients) on moderately large and relatively homogeneous customer groups. The demand factors are derived from recent historical data and modified in order to take into account technological, socio-economic or other influences. Forecasts of customer groups are obtained from independent agencies whose responsibility it is to produce them. The demand factors are then applied to the future values of constituent groups in order to obtain aggregate forecasts. This format of producing forecasts is consistent with best practices of demand forecasting by water utilities, and closely approximates the level of detail pursued in the local electric utilities.

#### TASK 2

Analyze unit production and flow factors with respect to WSSC property codes, service types and counties.

#### WSSC Design Manual

The Commission follows the practice of maintaining a Design Manual which covers the minimum standard criteria to be followed by design engineers when preparing plans and/or specifications for the construction of water and sewerage systems in the WSSD. It contains equations for developing demands for water and sewer services. Appendix D contains Flow Factors (coefficients) for use with those equations when applied to numerous types of water uses, including types of housing, and educational, retail and commercial properties. The same factors are to be used for both water demand and sewage flow forecasts, with no apparent allowance or differentiation for water main transmission losses, inflow/infiltration or other characteristics which distinguish between water and The use of these Factors might be improved by geographic differentiation and documentation refering to the method and date of their derivation. Appendices E and F contain Dwelling and Acreage Factors respectively for the various land use zoning classifications differentiated by County only. Again, there is no supporting information as to date or method of derivation.

#### Billing System Information

WSSC maintains relatively detailed customer records which contain the twelve most recent transactions and identify each account by property type (18 codes), service type (8 codes), regional location (200 ft sheet

number), and minibasin. More of this information could be used to develop locally disaggregate base factors for both water production and sewage flows.

Distribution System Storage Study (Project 6.02) June, 1980 Chapter IV of the report of this study contains an analysis of then-existing and projected water demands. The approach is thorough and the data and assumptions are well documented (i.e. future demands are based on Round II forecasts). The demands are disaggregated by distribution pressure zones or groups of zones. The results also include maximum day and peak hour factors and demands.

Water Production Report Through June, 1982 The purposes of this report include documenting historical water demand, presenting a procedure for determining water consumption for single family and multifamily residential and employment accounts, and developing data to be used for planning future Future demands are based on Round II improvements. results of the Cooperative Forecasting Program. price of water and weather are acknowledged as influencing the demand for water, although their effects are not explicitly taken into account in the examination or forecasting of demand. Analysis by pressure zone and type of account should be especially useful to the Commission in forecasting. The procedure developed for determining unaccounted for water by pressure zone should also be helpful in determining the effects of leak detection and elimination on water production. Now that the Round III cooperative forecasts of housing and employment are available, the intentions of producing periodic updating of the analysis should be carried out.

Residential Flow Factor Analysis (Contract No. 83MM1093-A)
This report describes a well documented project to update the derivation of sewage flow factors. It is dated November 1984, and is the first major analysis of flow factors since the work of Klein, reported in 1979. Flow factors are developed for four residential property codes and two composites of single and multifamily dwellings for the WSSD. Factors are also derived for inflow and infiltration. In addition, a factor was assumed in order to cover all uncertainties, including meter misregistration. This study explicitly takes into account the effects of weather by normalizing annual sewage flow with respect to

rainfall. It is indicated that sewage flows in recent years are less responsive to rainfall, which is perhaps due to successful system-wide efforts to reduce inflow and infiltration.

In summary, there is sufficient data and methodological information available at WSSC for the production of forecasts which are disaggregated on the basis of property codes, service types, and pressure zones. And, with the implementation of the sewer system model, it should be possible and desirable to develop some form of flow factors on a sewage drainage area basis. The degree of disaggregation should be determined by a study of the difference in water use and sewage characteristics among the classified codes, types and zones.

#### TASK 3

Analyze (and use where appropriate) the effects of changes in price and income.

On closer inspection of the WSSC rate schedule for both water and sewer services, and the variety of service types; time would not allow the level of detail necessary to address this task as it was originally set out. For instance, during the first year of the period of analysis, flat rates were charged for water and sewer services. During the remaining six years, a sliding scale on one hundred rate steps was in effect. Such rate schedules are notorious for confounding the price of a commodity under investigation.

In this case, the analysis might proceed by determining the quantity of water consumed and of sewer services required during each month in each service type. In this way, a weighted average price per month may be determined and compared with personal income and quantity of water consumed (and sewage generated). For reference and possible future application, data on personal percapita income and retail price index are provided in Tables 2 and 3.

TABLE 2 1976-1983 Personal Percapita Income Montgomery and Prince George's Counties

Ye	ear	Mont.	P. G. 's
19	97 6	10128	7005
19	977	11055	7749
19	978	12304	8490
19	979	13890	9361
19	980	15641	10400
19	981	16998	11172
19	982	18375	12031
1.0	983	19738	12939

TABLE 3 1976-1983 Washington Area Retail Price Index												
Yr	Jan	Feb	Mar	Apr	May	Jun	Jul	Aug	Sep	Oct	Nov	Dec
76		 178.4			182.2			185.	 5		188.1	
77	190.2		191.5		194.2		197.8		200.8		203.9	
78	208.7		212.6		216.0		220.4	22	222.9		225.4	
79	231.9		238.8		241.2		247.2		249.2		253.6	
80	257.2		262.3		264.7		271.4		271.8		275.5	
81	278.0		278.8		278.4	135	281.3		286.5		286.3	
82	289.0		289.0		292.6		296.8		300.9		302.7	

83 303.7 305.1 305.7 308.3 313.0 319.2

The work of Thomas M. Fischer of the Secretary's Office indicates that consumption in both commercial and single family residential accounts has shifted toward lower usage successively between the winters of '76-'77 and '80-'81, and between '80-'81 and '81-'82. No account appears to have been taken of differences in weather patterns which may have affected consumption during these years.

Other reports by McGarry and Brusnighan, Arthur P. Brigham, and others tend to confirm the move toward lower consumption since the introduction of the Conservation Orientated Rate Structure in January 1978.

Thus, there has been some analysis of the effect of price and rate structure on production of water at WSSC, but it has been sporadic and inconsistent. There is, however, no straightforward methodological analysis applicable in a case with a rate structure as complex as this one. Any attempt at analysis should clearly state the assumptions which are made.

#### TASK 4

Investigate and incorporate uncertainty due to weather into water production and sewage flow forecasting techniques.

"As far as the laws of mathematics refer to reality, they are not certain; and as far as they are certain, they do not refer to reality." Einstein

Having regard for Einstein's reflections on the applicability of uncertainty, it is still good practice to describe future expectations in terms of their likelihood of realization. WSSC forecasting capability and practice for water and sewer services includes the use of exceedence probabilities of moisture deficit in short term revenue forecasting, and normalization with respect to rainfall in sewage flow forecasting. The moisture deficit information was developed by consultants in 1980 and has experienced some problems with credibility and implementation, although the concept of exceedence probabilities is gaining acceptance in some areas. The rainfall normalization analysis of sewage flows was carried out by Bruce T. Downes of the Planning and Engineering Division and described in reports dated November 1984. These are good examples of how, by removing some of the effects of weather, the underlying pattern of sewage flow is exposed for further analysis and forecasting.

Further investigation was carried out as part of the present work in order to confirm the relationships between weather and the demand for services. Water production, sewage flow, rainfall and temperature data were collated for analysis. Monthly data were examined for the years 1977-1984. Plots of water vs sewage, and water and sewage vs rainfall and temperature were prepared (Figures 1 - 5). This type of data presentation is often useful in developing lines of further investigation. Clear relationships are seen between water and sewage, rainfall and water, and rainfall and sewage.

FIGURE 1 1977-1984 Water Production and Sewage Flow

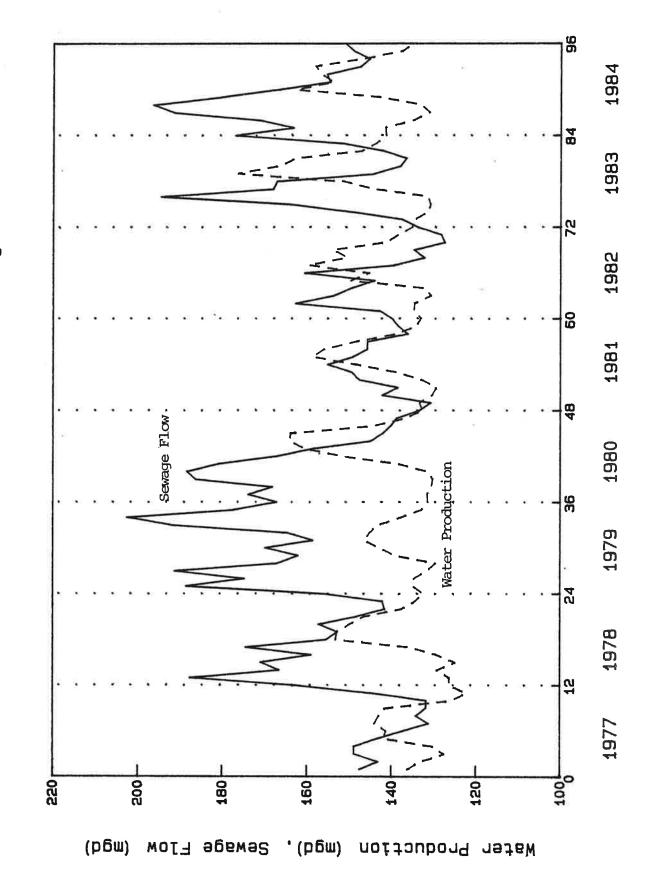


FIGURE 2 1977–1984 Water Production and Precipitation

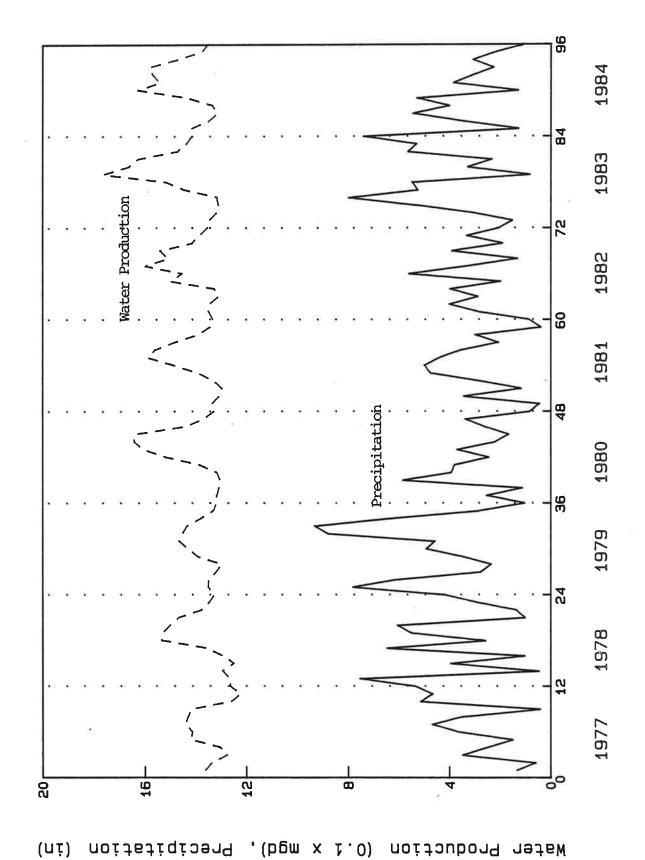


FIGURE 3 1977–1984 Water Production and Temperature

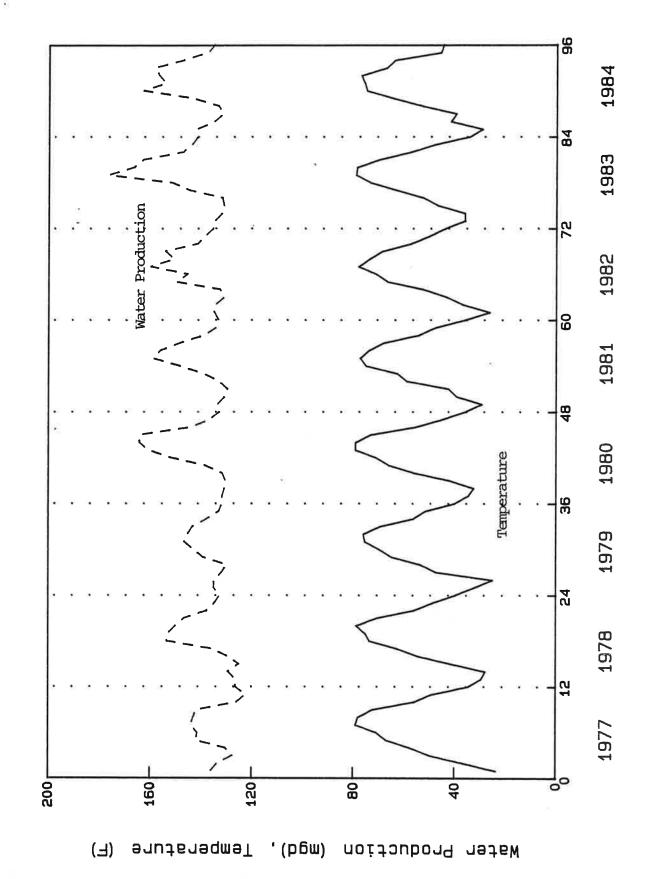
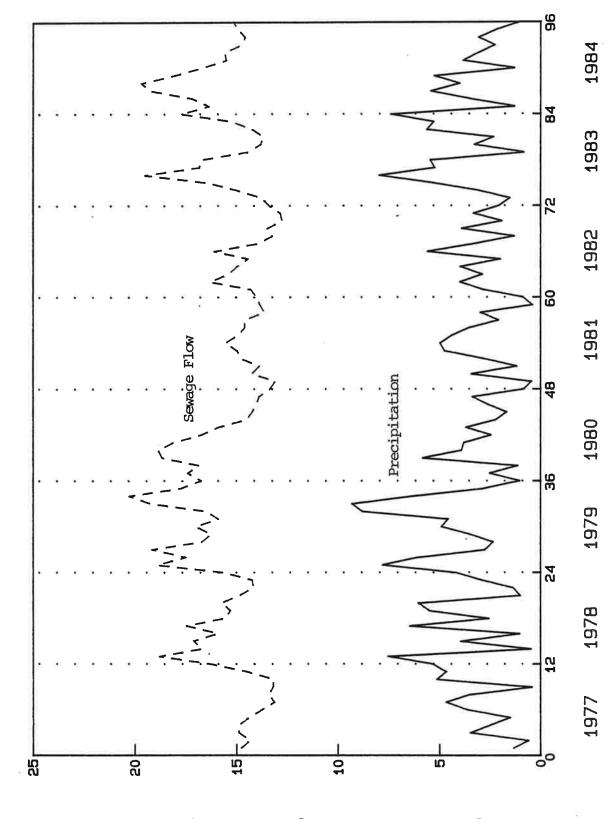


FIGURE 4 1977-1984 Sewage Flow and Precipitation



- 55 - Sewage Flow (0.1 x mgd), Precipitation (in)

FIGURE 5 1977–1984 Sewage Flow and Temperature Sewage Flow Temperature 250<sub>r</sub> 

- 23 -

Sewage Flow (mgd),

Temperature

(L)

Statistical correlations of monthly and annual data indicated that 1977 was an outlier, especially in water production data. It is always a matter of some judgement as to how long a period of historical record should be analyzed when deriving functional relationships to be used in forecasting. In general it should be as long as possible, provided that influential changes in the explanatory variables can be taken into account. In this case the rate structure underwent a significant change in January 1978 with appreciable antecedent publicity. Without further analysis, which is beyond the scope of this study, it is difficult to assess the effect of that change, and because it coincided with only the first year chosen for investigation, 1977 data might be dropped from further consideration.

The influence of both rainfall and temperature could be seen to vary through the year, i.e. heavy rainfall in early spring produces a greater response in sewage flow than a similar quantity of rain in late summer. It was hoped to capture some of the quantitative effects of this phenomenon by comparing cumulative monthly average temperature and rainfall with average annual water production and sewage flows. The results of this analysis were disappointingly inconclusive, and no significant statistical inferences could be drawn.

The motivation for performing statistical analysis of this nature is the resulting quantification of uncertainty in past experience. This knowledge of uncertainty can then be transferred (with some degree of confidence) to forecasts of future expectations.

There is still considerable room for improvement in removing the effects of weather in past water production and sewage flow data prior to forecasting. The combined effects of rainfall and temperature could be analyzed by joint functions such as moisture deficit, the annual cycle and variations in evapotranspiration, and drought indices. With these unpredictable influences removed and explained in probabilistic terms, the underlying trends due to changes in demography, housing and employment could be more easily determined and predicted. More complete forecasts could then be produced by imposing the probabilistic influence of weather.

An example calculation of such a forecast is presented in the description of Task 7.

#### TASK 5

Obtain and incorporate alternate development scenarios.

The most appropriate source of alternate scenarios is the Cooperative Forecasting Program of Metropolitan Washington Council of Governments. The most recent (Round III) cooperative forecast does present alternate scenarios of future conditions. The definitions of the alternatives incorporate explicit assumptions for the three scenarios. A summary is reproduced here for example purposes (Table 4).

Detailed documentation of alternate scenario assumptions is also provided in <u>Estimates and Forecasts of Dwelling Units</u>, <u>Population and Employment in Prince George's County</u>, July 1981. These assumptions are applicable to Round II Cooperative Forecasts and are reproduced here for historical comparison (Tables 5 and 6).

#### TASK 6

Present examples of forecasts which are conditioned on discrete assumptions about the future.

This concept follows directly from the previous subject. A forecast which would result from the use of alternate development scenarios would have several values of future conditions at each point in time. For example: low, intermediate and high; based on documented assumptions about the explanatory variables. The WSSC document Flow Projections for Workload Indices presents forecasts based on 5 discrete assumptions about future conditions:

- 1. a 15 year trend extrapolation,
- 2. a 10 year trend extrapolation,
- 3. a 5 year trend extrapolation,
- 4. Round III Cooperative Forecast results, and
- 5. Workload Indices for FY 86 budget preparation.

Another example might be to use the alternate development scenarios from the Round III Cooperative Forecast for each of the counties in order to produce alternate forecasts for water and sewer services. These would have to take into account the fact that WSSC does not serve all the outlying county areas which are subject to the Cooperative Forecasts. If the county scenarios are adopted, three scenarios would be applicable to forecasts for each county. Thus, potentially expanding the number of forecasts to 9 for the WSSD. Some judgement must be exercised when constructing scenarios in order to keep the numbers manageable. Perhaps in this case, forecasts for the WSSD could be based on scenarios limited to high/high, med/med, and low/low for the two counties, respectively.

## rable 4

# SUMMARY OF SCENARIOS

HIGH GROWTH SCENARIO	Foderal job growth assumption is the same as for the intermediate sconario.	Strong growth in information-based employment causes structural shift to a more "high technology" region. Services, transportation/communications/utilities and manufacturing sectors all experience much higher rates of growth than under other scenarios.	Overall strong growth in jobs causes strong population increase.	Construction of now housing and commercial buildings reaches highest levels.	Such strong job growth that in- migration reaches highest historic levels, mostly to burgeoning suburban employment centers.	Strong national economy with high rates of real growth in ail soctors.	Unemployment rate same as for intermediate scenario, indicating persistence of structural unemployment,	Same assumptions for multiple Job holding and self-employed (omitted) jobs as for inter- mediate scenario.
22	<b>-</b>	ni 🐃	e,	<b>.</b>	٠ <u>.</u>	•	7.	8
INTERMEDIATE GROWTH SCENARIO	foderal employment continues to decline until mid-1980s, then begins to grow again but at a lesser rate than in the past.	Steady growth of employment in services and rotall trade sectors, as well as in other sectors; modest growth in manufacturing jobs.	Overall moderate pace of job and population growth.	Housing and commercial construction resume healthy pace.	Continued in-migration to region due to growth in suburban employment centers.	National economic recovery continuos with an abating of inflationary pressures.	Uncmployment rate lower than national rate and declines as more jobs are created in all sectors.	More people working two jobs, fewor self- employed people due to healthy economy.
1	<b>:</b>	۸i .	m	÷	ស	•	•	é
LOW GROWTH SCENARIO	Continued decline in Federal cuployment until 1987, then stabilizing.	A slowdown in the rapid growth in services sector jobs, sluggish growth in others; decline in manufacturing after 1990.	Overall lower pace of job growth, and therefore lower, population increase.	Low lovel of housing and commercial construction.	Less in-migration to region due to poor employment growth prospects.	A lossening of national economic recovery and return to cycles of recession and high inflation.	Unomployment rate higher than traditional regional levels, more akin to national rate.	Lowor rate of multiple job holding, more self-employed poople.
	÷			÷	ري د	. 9	7.	<b>.</b>

#### DWELLING UNIT SUMMARY METHODOLOGY

		20th WK L LICTHODOCSO.	100000
Period	LOW	INTERMEDIATE	HIGH Single-Family
1976 to 1980	Single-Family Same as intermediate.	Single-Family Completions estimated from Building Permits equation (70-76) from 1977 and 1978. 1979 completions is average 1977 and 1978.	• Same as intermediate.
	Multifamily Same as intermediate.	Multifamily Completions estimate. from sewer authorizations to 1980 excluding any with legal or site plan problems.	Multifamily Same as intermediate.
	Single-Family	Single-Family	Single-Family
1980 to 1985	• Completions are extrapolocation of 1970-1976 rate of growth.	<ul> <li>Completions are the average of the extrapolation of short term and longer term trends.</li> </ul>	o Completions are extrap- clation of 1960-1977 rate of growth.
	Multifamily Completions based on the 1977-1980 annual average of sewer authorizations excluding the ones with any problems associated.	Multifamily  Average of the low and high rates.	Multifamily Completions based on the 1977-1980 average sewer authorizations.
	Single-Family	Single-Family	Single-Family
1985 to 1990	• Completions are extrap- olation of 1970-1976 rate of growth-	<ul> <li>Completions are the annual average rate of completions 1960-1977.</li> </ul>	<ul> <li>Completions are extrap- olation of 1960-1977 rate of growth.</li> </ul>
*	Multifamily Completions based on these units being 40% of the housing stock.	Multifamily Completions are based on the 1977-1980 average sewer authorizations.	Multifamily Residentially determined assuming Prince George's maintains 21% of region's housing (less 5,000 units to smooth the curve).
1990 to 1995	Single-Family Completions are extrapolation of 1970-1976 rate of growth.	Single-Family Completions are the annual average rate of completions 1960-1977.	Single-Family Completions are extrapolation 1960-1977 rate of growth.
ħ	Multifamily  • Completions based on these units being 39% of the stock.	Multifamily Completions are based on the 1977-1980 average sewer authorizations.	Multifamily Residentially determined assuming Prince George's maintains 21% of region's households.
1995 to 2000	Total Units Completions based on Prince George's maintaining a constant share of a growing region.	Single-Family Completions are the annual average rate of completions 1960-1977.	Single-Family Completions are extrapolation of 1960-1977 rate of growth.
1995 to 2000	Single-Family  The residual after subtracting multi-family units.	Multifamily Completions are based on the 1977-1980 average sewer authorizations.	• Residually determined assuming Prince George's maintains 21% of regional households.
	<ul> <li>Multifamily</li> <li>Completions based on the units being 38% of the housing stock.</li> </ul>	se	

TABLE 6

#### SUMMARY METHODOLOGY OF EMPLOYMENT ALTERNATIVES BY YEAR

	Low	Intermediate	High
1980 and 1985		1 Department of State Planne ent Projections	ing
1990	Share Analysis low at 15.7% of the region	Share analysis high at 15.7% of the region	Ratio of population/ employment improves to 2.47% or 0.70% of the region
כעען	Snare analysis low at 16.4% of the region	Ratio of population/ employment is 2.25% or 0.73% of the region	Share analysis high at 16.4% of the region
200ù	Share analysis low at 16.9% of the region	Ratio of population/ employment is 2.13% or 0.74% of the region	Share analysis high at 16.9% of the region
SOURCE:	"Recommended Forecasts Approval for Submission	George's County Council, Dec s of Population, Households on to COG and for Use in Pri y Planning Department, Resea	and Employment for nce George's County".

#### TASK 7

Present example probabilistic forecast in terms of probabilities of exceedence.

Most water demand forecasts are deterministic in that they provide only one scenario. Typically, no attempt is made to assign any level of likelihood to these forecasts whereas water use does contain random components. The randomness (uncertainty) of water use can be quantified in the form of a classical probability distribution which is derived from historical data and applied to expected (base) future demand. Given this information, water system managers are better equipped to make decisions as to the level of risk with which to The presentation of water use and sewage flow as stochastic phenomena impacts all other aspects of demand forecasting: price effects, conservation measures, revenue estimation, effects of weather, system planning, etc. following example the historic probability distribution is derived for sewage flow and a forecast is presented as being within confidence limits and as being below probabilities of Either or both of these presentation formats may be exceedence. applicable.

Base forecasts (sewage flow factors and water production factors times numbers of units) should have the same interpretation as the historic normalized data. After determining the probability density function from the historic data, it is applied at selected levels to the base forecast in order to produce forecasts which are explicitly probabilistic.

In this example, the work of Downes (1984) on sewage flow forecasts is extended as a probabilistic forecast. Nine years of data are used in the derivation of the probability distribution.

A regression of the Normalized Flows on 2-digit FY's (eg 77,78) produces the following information:

$$Reg_Normal = 12.7 + 1.74FY \tag{1}$$

		ST. DEV.	T-RATIO =
COL UMN	COEFFICIENT	OF COEF.	$\infty EF/S.D.$
	12.73	24.50	0.52
FΥ	1.7367	0.3023	5.75

Standard Error = 2.342

R-SQUARED = 82.5 PERCENT

R-SQUARED = 80.0 PERCENT, ADJUSTED FOR DEGREES OF FREEDOM Correlation Coefficient = 0.9083

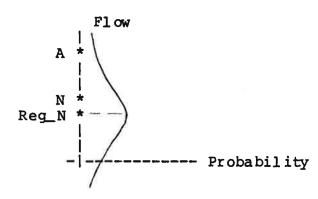
Thus, now for each FY, there are values for actual flow, normalized flow, and a point on the regression line of normalized flows (Reg\_Normal).

TABLE 7 1977-1985 Normalized Sewage Flow Data

FY	Sewage Flow	Water Consumed	Normal iz ed Sewage	Regressed Norm. Sew.	NFFadj
77	147.20	137.5	148.2	146.7	0.9966
78	154.20	133.4	146.5	148.5	0.9630
79	162.62	138.9	149.4	150.2	0.9236
80	177.22	137.4	154.4	152.0	0.8577
81	143.44	142.9	153.6	153.7	1.0715
82	147.32	141.3	152.5	155.4	1.0548
83	148.01	142.1	153.6	157.2	1.0621
84	163.24	148.5	159.6	158.9	0.9734
85	151.75	146.2	162.8	160.7	1.0590

With this information, adjusted normalized flow factors (NFFadj) are calculated for each year by equation 2.

In any particular year;



Reg\_N is the estimate (regression value) of normalized flow, and the actual flow value is assumed normally distributed about that estimate of N in a random manner due to the effects of

precipitation. Thus the quantification of the probability distribution of NFFadj is required in order to produce the transformation from Reg\_N to Actual Flow. <u>Under the assumption of being normally distributed</u>, the mean (NFFadj) and standard deviation (sNFFadj) are required.

In this case:  $\frac{\text{NFFadj}}{\text{NFFadj}} = 0.99576$ sNFFadj = 0.073735

The fundamental relationship (from Downes, 1984) is contained in equation 3.

In order to introduce probability into the calculation of Actual Flows, equation 3 is modified to the form given in equation 4.

$$\begin{array}{c} \text{Reg\_Normal} \\ \text{Actual Flow(p)} = -\underline{-----} \\ \text{NFFadj} \pm \text{t(p)sNFFadj} \end{array}$$

Where, t(p) is a standard normal factor selected at a desired level of probability (p) from a table of standard normal distribution function values. Table 8 is reproduced here for reference.

The solution to equation 4 provides the range of values about the regression line of Normalized Flow within which the Actual Flow is expected to fall with the probability (p) associated with the selected t(p) value.

Referring to Table 8, and requiring an interval within which Actual Flows are 90% likely to fall, t(p) values of  $\pm 1.645$  are selected. Similarly, for an 80% probability (or confidence) interval,  $t(p) = \pm 1.282$ . Upper and lower interval values for the 90% and 80% confidence levels are given in Table 9. In some forecast applications, the lower interval values may be of little significance, and only the upper limit is of importance to decision-making. The standard function Table 8 contains cumulative probability density function values; therefore, the Actual Flow values with a 5% probability of exceedence are given by the upper 90% interval values, see Figure 6, and those with a 10% probability of exceedence are given by the upper 80% interval values, and so on.

It should be noted that the interval values diverge, that is, the confidence bands are not parallel. This condition follows from Equation 4 for flow values at selected levels of confidence. An algebraic example illustrates this point:

$$Au = ---- D- Al = ---- D+$$

where:

Au, 1 = flow in an earlier year at upper and lower confidence levels

A'u, l = flow in a later year at upper and lower confidence levels

c = the increment by which RN increases between
 the earlier and the later year

RN = regressed normalized flow

 $D+_{,-}$  = denominator with + or - applicable.

The confidence interval in the earlier year would be:

and the confidence interval in the later year would be:

$$A'u - A'1 = \frac{RN + c}{D-} - \frac{RN + c}{D+}$$

The confidence interval is diverging if:

$$[(A'u - A'1) - (Au - Al)] > 0$$

Test:

Yes, since the term with the smallest denominator (D-) is greater than the term with the larger denominator (D+). The condition may be explained further by the fact that the confidence level flow values (Equation 4) are derived by a ratio whose denominator is the sum or difference of two constants, while the numerator increases through time.

For clarity, Figure 6 shows the relation among cumulative probability, confidence interval, and probability of exceedence.

FIGURE 6 Relation among Cumulative Probability, Confidence Interval, and Probability of Exceedence

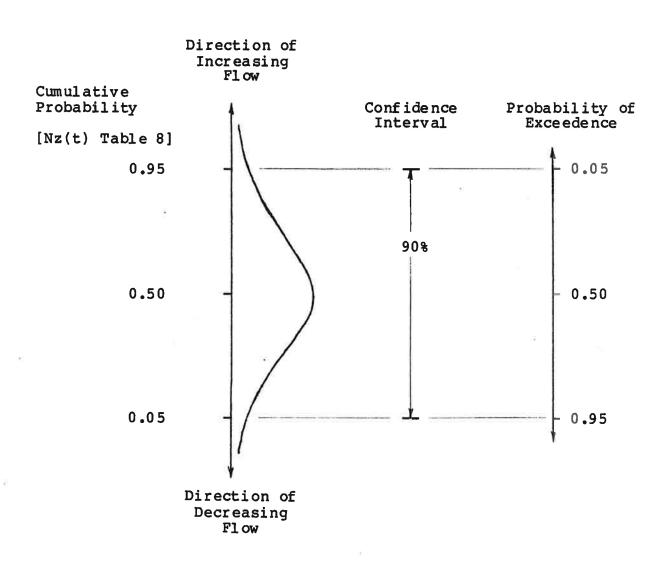


TABLE 8

Standard Normal Distribution Function

$$N_Z(t) = \int_{-\infty}^{t} \frac{1}{\sqrt{2\pi}} e^{-3t/2} dx$$

																												6
		(4)																										
م		.0014 .0019	.0026	.0048	2006	4000 4000 4000 4000 4000	.0143	.0183	.0233	.0294	.0367	.0455	.0559	1890.	.0823	.0985	.1170	.1379	1191.	.1867	.2148	.2451	2776	.3121	,3483	.3859	.4247	4641
-		.0014	.0027 .0037	9049	9900	) (800 (110 (110	.0146	.0188	.0239	.0300	.0375	.0465	.0571	.0694	.0838	.1003	.130	1401	.1635	.1894	7117	2483	.2810	.3156	.3520	7686.	.4286	.4681
1		.0015	.0028	.005	8900	9089	050.	.0192	.0244	.0307	.0384	.0475	.0582	.0708	.0853	1020	.1210	.1423	.1660	1921	2206	.2514	.2843	3192	.3557	.3936	.4325	.4721
9		.0015	.0029	.0052	6900.	99. 19. 5.	.0154	.0197	.0250	.0314	.0392	.0485	.0594	.0721	6980.	.1038	.1230	.1446	.1685	.1949	.2236	.2546	.2877	.3228	.3594	.3974	4364	.4761
2		.0016	0030 0040	.005 <b>4</b>	.007	2009 2009 2009	.0158	.0202	.0256	.0322	.0401	.0495	9090	.0735	.0885	.1056	1251	.1469	11711	1761.	.2266	.2578	.2912	.3264	.3632	.4013	404	.4801
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6		.0017	.0032 .0043	.0057	.0075	9600	.0166	.0212	.0268	.0336	.0418	9150.	.0630	.0764	8160.	.1093	.1292	.1515	.1762	2033	2326	2643	.2981	.3336	3707	4090	.4483	.4880
7		.0017	8. 8. 8. 8. 8.	.0059	.0078	2010.	0.05	.0217	.0274	.0344	.0427	.0526	.0643	.0778	.0934	.1112	.1314	.1539	1788	2061	2358	2676	3015	3372	3745	4129	4522	.4920
-		.001 <b>8</b> .0025	.0034 24 24 24	0900.	.0080	.0104	.0174	.0222	.0281	.0351	.0436	.0537	.0655	.0793	.0951	.1131	.1335	.1562	1814	2090	2389	2709	.3050	3409	3783	4168	.4562	.4960
0	.0013	.0019	.0035	.0062	.0082	.0107	6210.	.0227	.0287	.0359	.0446	.0548	.0668	.0808	8960	11151	.1357	.1587	1841	2119	2420	2743	3085	1446	1821	4207	4602	.5000
-	ij	-2.9	-2.6	-2.5	-2.4	-2.3	-2.1	-2.0	-1.9	 	-1.7	-1.6	-1.5	4.	-	-1.2	=	0.1	ı	) 00 	, ,			4	-	י רו	! -;	0

Standard Normal Distribution Function (continued)

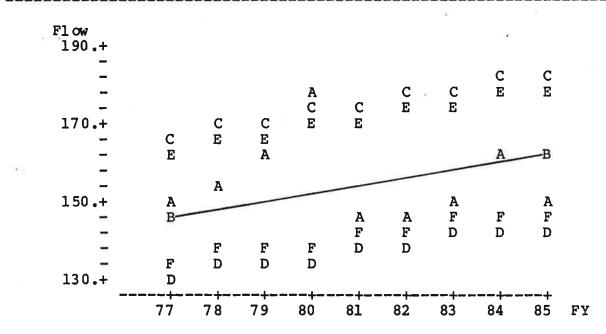
0.         5000         5040         5080         5120         5199         5239         5279         5319         5353           1.         5398         5438         5478         5317         5557         5536         5636         5675         5714         5753           2.         5793         5832         5871         5537         5536         5636         5617         5617         5714         5753           3.         6179         6217         6284         6528         6664         6700         6712         6064         6103         6141           3.         6179         6217         6628         6664         6700         6712         6064         6810         6517           4.         6180         6521         6664         6700         6712         6604         6810         6517           8.         7.	5000 5040 5080 5110 5160 5199 5239 5279 5119 5139 5373 5832 5438 5478 5517 5557 5596 5656 56054 56103 5617 56179 56179 56217 5625 56293 56311 56368 5646 5606 56443 5640 5619 5617 5628 5664 5670 5736 5772 5725 5629 5629 5631 56311 56368 5406 56443 5640 56172 5628 5684 5684 5628 5664 5670 5735 77257 7729 77257 7	-	•	-	77	e	4	<b>~</b>	•	7	<b></b>	6
5398         5438         5478         5517         5557         5556         5616         5617         5713         5714         5715         5717         5571         5571         5571         5571         5793         5812         5871         5871         5817         5817         5817         5617         6626         6604         66103         6613         66443         6614         6103         6614         6103         6614         6103         6614         6103         6614         6103         6614         6103         6614         6103         6614         6103         6614         6103         6614         6103         6614         6103         6614         6103         6614         6103         6614         6103         6614         6103         6614         6103         6614         6103         6614         6103         6614         6103         6103         <	5398         5438         5478         5517         5557         5556         5615         5615         5713         5714         5793         5812         5871         5811         5517         5557         5557         5617         6026         5610         5617         6626         5610         5618         5646         5610         5611         6628         6649         5610         6613         6644         6610         6613         6644         6610         6611         6644         6610         6611         6644         6610         6644         6610         6644         6610         6644         6610         6644         6610         6644         6610         6644         6610         6644         6610         6644         6610         6644         6610         6644         6610         6644         6610         6644         6610         6644         6610         6644         6610         6644         6610 <th< td=""><td>Q</td><td>5000</td><td>.5040</td><td>.5080</td><td>.5120</td><td>.5160</td><td>.5199</td><td>.5239</td><td>.5279</td><td>.5319</td><td>.5359</td></th<>	Q	5000	.5040	.5080	.5120	.5160	.5199	.5239	.5279	.5319	.5359
5793         .5812         .5871         .5910         .5948         .5987         .6026         .6064         .6103           6179         .6217         .6253         .6231         .6136         .6406         .6441         .6480           .6534         .6528         .6624         .6700         .6716         .6717         .6481         .6480           .6515         .6528         .6624         .6700         .6716         .7134         .7187         .7190           .7231         .7231         .7337         .7389         .7124         .7784         .7821           .7830         .7611         .7642         .7673         .7704         .7714         .7784         .7784           .7831         .7910         .7934         .7704         .7714         .7714         .7784           .8813         .8818         .8907         .8289         .8315         .8340         .8865           .8849         .8865         .8888         .8907         .8925         .8944         .8962         .8980         .8997           .9032         .9049         .9066         .9082         .9093         .9115         .9111         .9142           .9042	5793         .5812         .5871         .5910         .5948         .5987         .6026         .6064         .6103           .6179         .6217         .6255         .6293         .6311         .6368         .6406         .6441         .6480           .6354         .6528         .6624         .6700         .6716         .7142         .7377         .7190           .7354         .7351         .7704         .7714         .7744         .7486         .7517           .7350         .7611         .7642         .7633         .7004         .7714         .7744         .7744         .7744           .7881         .7910         .7939         .7067         .7704         .7714         .7744         .7744         .7744         .7744         .7744         .7744         .7744         .7744         .7747         .7717         .7190           .8159         .7621         .7622         .8057         .8259         .8115         .8140         .8165         .8644         .7517         .7190           .8113         .8418         .8461         .8673         .8051         .8051         .8051         .8041         .8041         .8041         .8051         .8051         .8051	=	.5398	.5438	.5478	.5517	.5557	.5596	.5636	.5675	.5714	.5753
6517 6217 6225 6293 6311 6368 6406 6443 6480 6554 6554 6554 6559 6664 6700 6736 6772 6808 6844 6845 68915 6628 6664 6700 6736 6772 6808 6844 68915 68915 6892 8654 7722 7454 7786 7719 7717 7750 7750 7751 7750 7751 7750 7751 7750 7751 7751	6179 6217 6255 6293 .6311 6168 6406 6441 6480 6554 6554 6554 6559 6624 .6700 6715 6712 6808 6844 6854 6559 6528 .7019 .7054 .7088 .7123 .7157 .7190 .7257 .7251 .7324 .7357 .7389 .7422 .7454 .7486 .7714 .7823 .7881 .7910 .7934 .7957 .7955 .8023 .8021 .8079 .8106 .8105 .8106 .8158 .8289 .8315 .8340 .8365 .8166 .812 .8238 .8254 .8577 .8399 .8165 .865 .866 .8708 .8711 .8749 .8869 .8888 .8907 .8925 .8944 .8962 .8980 .8997 .9012 .9049 .9066 .9082 .9099 .9115 .9131 .9147 .9162 .9132 .9347 .9357 .9359 .9551 .9255 .9299 .9508 .9515 .9515 .9515 .9515 .9515 .9515 .9515 .9515 .9516 .9641 .9449 .9485 .9559 .9608 .9616 .9615 .9616 .9615 .9641 .9649 .9656 .9654 .9571 .9789 .9608 .9616 .9619 .9619 .9619 .9619 .9619 .9619 .9911 .9913 .9719 .9726 .9732 .9734 .9484 .9495 .9559 .9608 .9616 .9619 .9619 .9951 .9913 .9918 .9929 .9608 .9911 .9913 .9913 .9918 .9929 .9969 .9961 .9911 .9913 .9918 .9929 .9969 .9961 .9911 .9913 .9918 .9929 .9969 .9911 .9913 .9918 .9929 .9961 .9911 .9913 .9928 .9920 .9921 .9929 .9921 .9911 .9913 .9928 .9920 .9921 .9921 .9931 .9931 .9935 .9926 .9926 .9920 .9921 .9921 .9931 .9935 .9926 .9926 .9920 .9921 .9921 .9931 .9935 .9926 .9926 .9920 .9921 .9921 .9931 .9935 .9926 .9926 .9920 .9921 .9921 .9931 .9935 .9936 .9926 .9926 .9920 .9921 .9931 .9931 .9932 .9926 .9926 .9926 .9926 .9920 .9921 .9931 .9931 .9932 .9936 .9936 .9926 .9926 .9926 .9926 .9926 .9927 .9928 .9926 .9927 .9928 .9926 .9929 .9931 .9931 .9932 .9936 .993	ų	.5793	.5832	.5871	.5910	.5948	.5987	9709.	.6064	.6103	.6141
6554         6559         6664         6700         6716         6712         6808         6844           6915         6950         6985         7019         7054         7088         7123         7157         7190           7727         7291         7324         7359         7422         7434         7764         7734           7880         7611         7642         7753         7704         7734         7764         7794         7823           7881         7910         7939         7967         7795         8023         8051         8079         8106           8159         8186         8212         8238         8233         8315         8310         8316           8443         8465         8866         8708         8725         8744         8962         8810           8443         8655         8868         8907         8225         8944         8962         8990           9012         9029         9115         9110         9141         9444         9495         9505         9513         970           9132         9132         9132         9513         9544         9495         9505         9506	6554         6559         -6664         -6700         -6716         -6712         -6808         -6844           6915         -6926         -6664         -6700         -6716         -7712         -7717         -7719           -7727         -7721         -7722         -7424         -7746         -7794         -7719           -781         -7711         -7744	L.	6119.	.6217	.6255	.6293	1663.1	.6368	.6406	.6443	.6480	.6517
.6915         .6926         .7019         .7054         .7088         .7123         .7157         .7190           .7257         .7251         .7357         .7359         .7422         .7454         .7486         .7517           .7250         .7511         .7543         .7764         .7744         .7764         .7794         .7813           .7881         .7610         .7939         .7967         .7995         .8023         .8051         .8079         .8106           .8159         .8186         .8212         .8258         .8251         .8541         .8340         .8106           .8143         .8866         .8708         .8729         .8749         .8770         .8790         .8110           .8643         .8865         .8708         .8729         .8749         .8877         .8890         .8907         .8909         .9115         .9111         .9147         .9162         .9990         .9115         .9111         .9147         .9162         .9994         .8962         .9990         .9115         .9114         .9484         .9495         .9505         .9279         .9106         .9916         .9916         .9916         .9916         .9916         .9916 <td< td=""><td>.6915         .6950         .6985         .7019         .7054         .7088         .7123         .7157         .7191           .7257         .7251         .7342         .7454         .7486         .7517         .7164         .7187         .7164         .7187         .7164         .7187         .7164         .7187         .7164         .7187         .7164         .7187         .7164         .7187         .7164         .7187         .7164         .7187         .7164         .7187         .7164         .7187         .7164         .7187         .7164         .7187         .7164         .7187         .8186         .8106         .8102         .8051         .8051         .8051         .8053         .8051         .8053         .8051         .8059         .8166         .81</td><td>4</td><td>.6554</td><td>.6591</td><td>.6628</td><td>.6664</td><td>.6700</td><td>.6736</td><td>.6772</td><td>.6808</td><td>.6844</td><td>6899</td></td<>	.6915         .6950         .6985         .7019         .7054         .7088         .7123         .7157         .7191           .7257         .7251         .7342         .7454         .7486         .7517         .7164         .7187         .7164         .7187         .7164         .7187         .7164         .7187         .7164         .7187         .7164         .7187         .7164         .7187         .7164         .7187         .7164         .7187         .7164         .7187         .7164         .7187         .7164         .7187         .7164         .7187         .7164         .7187         .8186         .8106         .8102         .8051         .8051         .8051         .8053         .8051         .8053         .8051         .8059         .8166         .81	4	.6554	.6591	.6628	.6664	.6700	.6736	.6772	.6808	.6844	6899
.7257 .7291 .7324 .7357 .7389 .7422 .7454 .7486 .7517 .7580 .7611 .7642 .7673 .7704 .7734 .7764 .7794 .7795 .8015 .8019 .8106 .8116 .7813 .7910 .7939 .7967 .7995 .8023 .8051 .8079 .8106 .8159 .8186 .8212 .8238 .8264 .8289 .8315 .8340 .8365 .8043 .8051 .8079 .8106 .8043 .8065 .8086 .8708 .8729 .8749 .8770 .8790 .8810 .8849 .8869 .8888 .8907 .8225 .8944 .8962 .8980 .8997 .8012 .9049 .9066 .9082 .9099 .9115 .9131 .9147 .9162 .9192 .9207 .9222 .9236 .9251 .9265 .9279 .9222 .9306 .9418 .9429 .9554 .9564 .9573 .9370 .9382 .9594 .9686 .9616 .9625 .9513 .9452 .9464 .9564 .9573 .9781 .9599 .9608 .9616 .9625 .9513 .9454 .9564 .9573 .9784 .9591 .9599 .9608 .9616 .9625 .9513 .9713 .9719 .9712 .9738 .9731 .9738 .9744 .9750 .9756 .9761 .9073 .9713 .9719 .9722 .9934 .9838 .9942 .9846 .9863 .9911 .9913 .9914 .9918 .9824 .9884 .9884 .9888 .9911 .9913 .9926 .9909 .9911 .9913 .9918 .9926 .9926 .9926 .9926 .9926 .9926 .9926 .9926 .9926 .9926 .9926 .9926 .9926 .9929 .9911 .9913 .9938 .9938 .9938 .9938 .9938 .9938 .9938 .9939 .9936 .9936 .9936 .9936 .9936 .9936 .9936 .9936 .9936 .9936 .9936 .9937 .9938 .9936	.7257 .7291 .7324 .7357 .7389 .7422 .7454 .7486 .7517 .7580 .7611 .7642 .7673 .7704 .7734 .7764 .7794 .7734 .7764 .7794 .7823 .7811 .7910 .7939 .7967 .7995 .8023 .8051 .8079 .8106 .8159 .8186 .8212 .8238 .8264 .8289 .8315 .8340 .8365 .8106 .8212 .8238 .8264 .8289 .8315 .8340 .8365 .8643 .8665 .8686 .8708 .8729 .8749 .8770 .8790 .8810 .8849 .8869 .8888 .8907 .8925 .8944 .8962 .8980 .8997 .9012 .9049 .9066 .9082 .9099 .9115 .9131 .9147 .9162 .9192 .9207 .9222 .9236 .9251 .9265 .9279 .9292 .9306 .9412 .9452 .9464 .9484 .9495 .9505 .9519 .9529 .9516 .9524 .9554 .9564 .9571 .9589 .9608 .9616 .9625 .9511 .9713 .9719 .9726 .9732 .9738 .9798 .9908 .9608 .9616 .9625 .9511 .9713 .9719 .9726 .9732 .9734 .9744 .9750 .9756 .9761 .9733 .9726 .9874 .9874 .9878 .9871 .9878 .9878 .9878 .9878 .9878 .9878 .9878 .9878 .9878 .9878 .9878 .9879 .9909 .9911 .9913 .9918 .9920 .9921 .9924 .9926 .9966 .9966 .9966 .9966 .9967 .9926 .9921 .9929 .9911 .9913 .9928 .9956 .9966 .9967 .9929 .9911 .9911 .9913 .9928 .9956 .9967 .9929 .9911 .9913 .9928 .9956 .9967 .9929 .9911 .9913 .9929 .9951 .9929 .9911 .9913 .9929 .9951 .9929 .9951 .9921 .9938 .9956 .9966 .9967 .9968 .9967 .9928 .9960 .9961 .9976 .9978 .9979 .9978 .9978 .9978 .9978 .9978 .9978 .9978 .9978 .9979 .9979 .9971 .9977 .9978 .9974 .9978 .9978 .9978 .9978 .9978 .9978 .9978 .9978 .9978 .9978 .9978 .9978 .9978 .9978 .9978 .9978 .9978 .9979 .9978 .9978 .9978 .9978 .9978 .9978 .9978 .9978 .9978 .9978 .9979 .9978	'n	\$169.	.6950	.6985	.7019	.7054	.7088	.7123	7317.	.7190	.7224
7580         7611         7642         7673         7704         7714         7764         7794         7784         7784         7784         7784         7784         7784         7784         7787         7785         8023         8051         8079         8106           8159         .8186         .8212         .8238         .8264         .8289         .8115         .8106         .8106           .8413         .8466         .8708         .8729         .8289         .8315         .8340         .8106           .8643         .8665         .8686         .8708         .8729         .8749         .8970         .8106           .8643         .8665         .8686         .8708         .9099         .9115         .9131         .9147         .9162           .9012         .9049         .9015         .9159         .9046         .9046         .9046         .9046         .9046         .9046         .9046         .9048         .9046         .9046         .9046         .9046         .9046         .9046         .9046         .9046         .9046         .9046         .9046         .9046         .9046         .9046         .9046         .9046         .9046         .9046	7580         7611         7642         7673         7704         7734         7764         7794         7784         7764         7794         7784         7784         7784         7784         7781         7881         7881         7881         7892         7815         8805         8816         8818         88212         8828         8828         8861         8789         8811         8854         8862         8880         8907         8810 <t< td=""><td>_</td><td>7257</td><td>7291</td><td>.7324</td><td>7357</td><td>.7389</td><td>.7422</td><td>.7454</td><td>.7486</td><td>71517.</td><td>.7549</td></t<>	_	7257	7291	.7324	7357	.7389	.7422	.7454	.7486	71517.	.7549
.7881         .7910         .7939         .7967         .7995         .8023         .8051         .8079         .8106           .8159         .8186         .8212         .8238         .8264         .8289         .8315         .8106         .8105           .8413         .8466         .8665         .866         .8708         .8729         .8311         .8554         .8340         .8365           .8643         .8665         .8686         .8708         .8729         .8729         .8116         .8749         .8790         .8106           .8643         .8665         .8686         .8907         .8925         .8944         .8962         .8990         .8962           .9032         .9049         .9155         .9279         .9116         .9147         .9162           .9132         .9347         .9484         .9495         .9506         .9406	.7881       .7910       .7939       .7967       .7995       .8023       .8051       .8105       .8105         .8159       .8186       .8212       .8238       .8264       .8289       .8315       .8105       .8105         .8643       .8655       .866       .8708       .8731       .8554       .8777       .8395         .8643       .8655       .8686       .8708       .8729       .8749       .8710       .8795         .8643       .8655       .8686       .8707       .8925       .8944       .8962       .8990       .8910         .9032       .9049       .9066       .9082       .9099       .9115       .9131       .9147       .9162         .9032       .9249       .9156       .9244       .8962       .8960       .8961       .9962         .9452       .9247       .9484       .9495       .9265       .9269       .9608       .9616       .9625         .9541       .9542       .9541       .9542       .9548       .9686       .9608       .9616       .9625       .9531       .9799       .9608       .9616       .9625       .9531         .9541       .9542       .9544       .9644	_	.7580	7611	.7642	.7673	.7704	.7734	.7764	.7794	.7823	.7852
8159         8186         8212         8238         8264         8289         8315         8340         8365           8441         3865         3866         8708         8531         8534         8577         8359           8643         3865         3866         8708         8729         8749         8770         8990           8643         3865         3866         8907         8255         8944         8962         8810           8849         3865         3666         3082         3909         9115         9131         9147         9162           9032         9046         .9066         .9082         .9099         .9115         .9131         .9147         .9162           9132         .9271         .9251         .9265         .9664         .9671         .9678         .9686         .9616         .9625           .9541         .9549         .9656         .9664         .9671         .9744         .9750         .9735         .9736           .9713         .9719         .9726         .9732         .9738         .9744         .9750         .9756         .9716           .9713         .9719         .9776         .9744	8159         8186         8212         8238         8264         8289         8315         8340         8365           8443         8465         8461         8485         8508         8531         8554         8577         8599           8643         8665         8686         8708         8729         8713         8770         8790           8643         8665         8686         8708         8729         8731         8754         8870         8810           8649         8869         8888         8907         8925         8944         8962         8980         8990           9032         9049         9066         9082         9069         9115         9147         9162           9132         9347         9348         9495         9364         9495         9505         9518         9429           9452         9544         9543         9543         9544         9495         9506         9618         9616         9629         9616         9629         9616         9629         9616         9629         9616         9629         9616         9629         9616         9629         9629         9629         9629 <t< td=""><td>-</td><td>.7881</td><td>.7910</td><td>.7939</td><td>7967.</td><td>.7995</td><td>.8023</td><td>.8051</td><td>.8079</td><td>.8106</td><td>.8133</td></t<>	-	.7881	.7910	.7939	7967.	.7995	.8023	.8051	.8079	.8106	.8133
8413       .8438       .8461       .8485       .8508       .8531       .8554       .8577       .8599         .8643       .8665       .8666       .8708       .8729       .8749       .8770       .8790       .8810         .8849       .8865       .8866       .8708       .8725       .8944       .8962       .8907       .9810         .9012       .9049       .9066       .9082       .9099       .9115       .9131       .9147       .9147       .9117       .9147       .9167       .9167       .9167       .9167       .9167       .9167       .9167       .9179	8413       .8438       .8461       .8485       .8508       .8531       .8554       .8577       .8599         .8643       .8665       .8666       .8708       .8729       .8749       .8770       .8790       .8810         .8849       .8869       .8888       .8907       .8255       .8944       .8962       .8997       .9997       .9911       .9111       .9147       .9147       .9115       .9111       .9147       .9112       .9111       .9111       .9147       .9162       .9939       .9115       .9131       .9147       .9148       .9949       .9112       .9111       .9111       .9111       .9111       .9111       .9111       .9114       .9465       .9573       .9594       .9406       .9906       .9906       .9906       .99		.8159	.8186	.8212	.8238	.8264	.8289	.8315	.8340	.8365	.8389
3643       3665       3686       8708       8729       3749       38770       38190         3849       3869       3888       3907       3825       3844       3862       3880       3891         3849       3869       3888       3907       3825       3944       3862       3890       3891         3912       3904       3066       9082       3099       3115       3147       3162         3913       3948       3926       3926       3929       3929       3929       3929         3945       3945       3947       3948       3949       3946       3948       3948       3948       3948       3948       3948       3948       3948       3948       3948       3981       3984       3948       3981       3984       3984       3984       3984       3984       3984       3988       3981       3984       3988       3981       3988       3981       3984       3984       3988       3981       3984       3988       3981       3988       3981       3988       3981       3988       3981       3988       3981       3984       3988       3981       3988       3988       3988       <	8643       .8665       .8708       .8729       .8749       .8770       .8790       .8819         .8849       .8869       .8888       .8907       .8255       .8944       .8962       .8980       .8997         .9032       .9066       .9082       .9099       .9115       .9131       .9147       .9162         .9192       .9207       .9226       .9251       .9265       .9279       .9252       .9379         .9452       .9461       .9484       .9495       .9406       .9418       .9429         .9452       .9462       .9573       .9382       .9591       .9596       .9606       .9616       .9625         .9541       .9649       .9656       .9671       .9678       .9686       .9616       .9616       .9625         .9641       .9649       .9656       .9671       .9678       .9686       .9616       .970         .9713       .9719       .9718       .9744       .9750       .9716       .970         .9713       .9719       .9748       .9749       .9746       .9750       .971         .9821       .9822       .9831       .9842       .9846       .9846       .9841       .	0	.8413	.8438	.8461	.8485	.8508	.8531	.8554	.8577	.8599	.8621
.8849       .8869       .8888       .8907       .8925       .8944       .8962       .8980       .8991         .9012       .9049       .9066       .9082       .9099       .9115       .9131       .9147       .9162         .9192       .9204       .9066       .9082       .9099       .9115       .9131       .9147       .9162         .9132       .9207       .9236       .9256       .9279       .9295       .9209       .9182       .9379       .9668       .9616       .9625       .9535       .9508       .9616       .9625       .9636       .9671       .9678       .9686       .9616       .9625       .9636       .9616       .9625       .9638       .9616       .9625       .9638       .9616       .9678       .9686       .9616       .9625       .9638       .9616       .9678       .9686       .9616       .9625       .9638       .9761       .9744       .9750       .9756       .9761       .9761       .9744       .9750       .9756       .9761       .9761       .9744       .9750       .9817       .9817       .9818       .9818       .9818       .9818       .9818       .9818       .9818       .9818       .9818       .9818       .981	.8849       .8869       .8888       .8907       .8925       .8944       .8962       .8980       .8991         .9032       .9049       .9066       .9082       .9015       .9115       .9131       .9147       .9162         .9192       .9204       .9066       .9082       .9099       .9115       .9131       .9147       .9162         .9132       .9207       .9236       .9251       .9265       .9265       .9279       .9265       .9292       .9305         .9452       .9463       .9484       .9495       .9505       .9516       .9429         .9543       .9464       .9484       .9495       .9508       .9616       .9429         .9544       .9564       .9671       .9678       .9686       .9616       .9616       .9616       .9625       .9516       .9616       .9616       .9616       .9616       .9616       .9616       .9701       .9749       .9749       .9750       .9751       .9761       .9761       .9771       .9749       .9817       .9817       .9817       .9818       .9817       .9818       .9818       .9818       .9818       .9818       .9818       .9818       .9818       .9818       .9818	=	.8643	.8665	.8686	8078	.8729	.8749	.8770	.8790	.8810	.8830
.9032       .9049       .9066       .9082       .9099       .9115       .9131       .9147       .9162         .9192       .9207       .9236       .9251       .9265       .9279       .9292       .9306         .9132       .9245       .9357       .9376       .9382       .9394       .9406       .9418       .9429         .9452       .9463       .9484       .9495       .9505       .9505       .9515       .9525       .9318         .9452       .9463       .9484       .9495       .9508       .9616       .9625       .9531       .9599       .9608       .9616       .9625       .9635       .9636       .9616       .9625       .9631       .9700       .9719       .9744       .9750       .9756       .9761       .9744       .9750       .9751       .9761       .9761       .9744       .9750       .9761       .9761       .9761       .9761       .9761       .9761       .9773       .9744       .9750       .9761       .9761       .9761       .9761       .9761       .9762       .9871       .9884       .9881       .9881       .9881       .9881       .9884       .9881       .9881       .9881       .9881       .9881       .9881<	.9032       .9049       .9066       .9082       .9099       .9115       .9131       .9147       .9162         .9192       .9207       .9236       .9251       .9265       .9279       .9292       .9306         .9132       .9245       .9357       .9376       .9382       .9394       .9406       .9418       .9429         .9452       .9463       .9484       .9495       .9505       .9608       .9616       .9625         .9554       .9564       .9573       .9582       .9599       .9608       .9616       .9625         .9554       .9564       .9573       .9591       .9598       .9608       .9616       .9625         .9641       .9649       .9656       .9671       .9678       .9686       .9608       .9616       .9608         .9713       .9719       .9744       .9750       .9750       .9750       .9761       .9700         .9773       .9718       .9748       .9749       .9750       .9756       .9817       .9818       .9842       .9846       .9817       .9818       .9818       .9818       .9818       .9818       .9818       .9818       .9818       .9818       .9818       .9818	1.2	.8849	.8869	.8888	.8907	.8925	.8944	.8962	.8980	7668.	2005
.9192       .9207       .9236       .9231       .9265       .9292       .9306         .9332       .9348 \ .9370       .9382       .9394       .9406       .9418       .9429         .9452       .9463       .9484       .9495       .9505       .9515       .9525       .9535         .9452       .9463       .9484       .9495       .9506       .9618       .9418       .9429         .9554       .9564       .9573       .9581       .9599       .9608       .9616       .9625         .9641       .9649       .9656       .9671       .9599       .9608       .9616       .9625         .9641       .9649       .9656       .9671       .9678       .9686       .9608       .9616       .9608         .9713       .9719       .9744       .9750       .9750       .9761       .9761       .9761       .9761       .9761       .9761       .9761       .9761       .9874       .9881	.9192       .9207       .9236       .9231       .9265       .9292       .9306         .9332       .9348 \ .9370       .9382       .9394       .9406       .9418       .9429         .9452       .9463       .9474       .9484       .9495       .9505       .9515       .9525       .9535         .9554       .9564       .9573       .9582       .9591       .9608       .9616       .9625         .9641       .9649       .9656       .9654       .9671       .9578       .9686       .9616       .9625         .9713       .9719       .976       .9678       .9686       .9616       .9609       .9616       .9609         .9713       .9719       .9744       .9750       .9756       .9761       .9761       .9761       .9761       .9776       .9750       .9761       .9761       .9761       .9761       .9761       .9761       .9871       .9878       .9887       .9887       .9887       .9887       .9887       .9887       .9887       .9887       .9887       .9887       .9887       .9887       .9887       .9987       .9918       .9919       .9919       .9919       .9911       .9913       .9918       .9918       .991	1.3	.9032	.9049	9906	.9082	9006	.9115	.9131	.9147	.9162	.917
9332       .9345 \ .9357       .9370       .9382       .9394       .9406       .9418       .9429         .9452       .9463       .9474       .9484       .9495       .9505       .9515       .9525       .9535         .9554       .9564       .9573       .9591       .9599       .9608       .9616       .9615         .9641       .9649       .9656       .9664       .9671       .9678       .9686       .9616       .9615         .9641       .9649       .9656       .9664       .9671       .9678       .9686       .9616       .9610         .9713       .9719       .9718       .9744       .9750       .9756       .9761         .9713       .9718       .9718       .9744       .9750       .9756       .9761         .9821       .9834       .9818       .9842       .9846       .9861       .9871         .9861       .9864       .9878       .9881       .9884       .9881         .9861       .9868       .9978       .9846       .9867       .9867         .9861       .9950       .9910       .9910       .9911       .9911       .9911         .9918       .9946       .9946	9332 .9345 \ 9357 .9370 .9382 .9394 .9406 .9418 .9429 .9452 .9453 .9453 .9454 .9484 .9495 .9505 .9515 .9525 .9535 .9554 .9564 .9573 .9582 .9591 .9599 .9608 .9616 .9625 .9641 .9649 .9656 .9664 .9671 .9678 .9686 .9693 .9700 .9713 .9719 .9726 .9732 .9738 .9734 .9750 .9756 .9756 .9761 .9773 .9778 .9786 .9832 .9738 .9744 .9750 .9756 .9761 .9773 .9778 .9864 .9878 .9834 .9838 .9846 .9864 .9887 .9861 .9864 .9888 .9871 .9875 .9878 .9878 .9881 .9884 .9887 .9861 .9864 .9868 .9901 .9904 .9906 .9911 .9913 .9918 .9920 .9927 .9927 .9929 .9946 .9931 .9918 .9931 .9925 .9957 .9959 .9960 .9951 .9977 .9978 .9966 .9977 .9978 .9989 .9977 .9978 .9988 .9989 .9977 .9978 .9988	1.4	.9192	.9207	.9222	.9236	.9251	.9265	.9279	.9292	.9306	9319
9452       .9463       .9484       .9495       .9505       .9515       .9525       .9535         .9554       .9564       .9573       .9582       .9508       .9608       .9616       .9625         .9641       .9564       .9573       .9584       .9599       .9608       .9616       .9625         .9713       .9719       .9656       .9671       .9578       .9686       .9693       .9700         .9773       .9718       .9726       .9732       .9738       .9744       .9750       .9756       .9761         .9821       .9826       .9830       .9834       .9838       .9842       .9846       .9867       .9867         .9861       .9864       .9868       .9871       .9878       .9881       .9887       .9887         .9861       .9864       .9868       .9901       .9904       .9906       .9909       .9913       .9913       .9913         .9918       .9920       .9925       .9927       .9929       .9946       .9948       .9949       .9949       .9941         .9953       .9956       .9957       .9946       .9946       .9948       .9941       .9949       .9941       .9949       <	9452       .9463       .9484       .9495       .9505       .9515       .9525       .9535         .9554       .9564       .9573       .9582       .9501       .9599       .9608       .9616       .9625         .9641       .9649       .9656       .9651       .9578       .9686       .9616       .9625         .9713       .9719       .9656       .9671       .9678       .9686       .9616       .9605         .9713       .9719       .9744       .9750       .9750       .9761         .9773       .9778       .9784       .9784       .9786       .9766       .9766       .9767       .9767       .9769       .9817         .9821       .9826       .9839       .9871       .9878       .9881       .9884       .9887       .9887       .9887       .9887       .9887       .9887       .9887       .9887       .9887       .9999       .9906       .9919       .9919       .9913       .9913       .9913       .9913       .9913       .9913       .9914       .9914       .9914       .9914       .9914       .9914       .9914       .9914       .9914       .9914       .9914       .9914       .9914       .9914       .9914	¥	9112	9145	19357	9370	9382	9394	.9406	9418	9429	9441
.9554       .9564       .9573       .9582       .9599       .9608       .9616       .9625         .9641       .9649       .9656       .9671       .9678       .9686       .9693       .9700         .9713       .9719       .9726       .9732       .9738       .9744       .9750       .9756       .9761         .9773       .9778       .9781       .9783       .9793       .9794       .9750       .9756       .9761         .9821       .9826       .9830       .9834       .9836       .9846       .9867       .9854         .9861       .9864       .9868       .9971       .9878       .9881       .9887       .9887         .9861       .9862       .9901       .9904       .9906       .9906       .9911       .9913         .9918       .9920       .9927       .9927       .9929       .9946       .9948       .9949       .9941         .9938       .9940       .9948       .9949       .9946       .9946       .9946       .9946       .9946       .9946       .9946       .9946       .9946       .9946       .9946       .9946       .9946       .9946       .9946       .9946       .9946       .9946	.9554       .9564       .9581       .9599       .9608       .9616       .9625         .9641       .9649       .9656       .9671       .9678       .9686       .9693       .9700         .9713       .9716       .9726       .9671       .9678       .9686       .9693       .9701         .9713       .9718       .9726       .9732       .9738       .9744       .9750       .9756       .9761         .9773       .9778       .9781       .9784       .9784       .9766       .9766       .9766       .9766       .9766       .9766       .9766       .9766       .9766       .9876       .9876       .9876       .9881       .9981       .9913       .9913       .9913       .9913       .9913       .9914       .9914       .9914       .9914       .9914       .9914       .9914       .9914       .9914 </td <td>9.1</td> <td>9452</td> <td>.9463</td> <td>9474</td> <td>9484</td> <td>.9495</td> <td>.9505</td> <td>9515</td> <td>.9525</td> <td>.9535</td> <td>.954</td>	9.1	9452	.9463	9474	9484	.9495	.9505	9515	.9525	.9535	.954
.9641       .9649       .9656       .9654       .9671       .9678       .9686       .9693       .9700         .9713       .9719       .9726       .9732       .9738       .9744       .9750       .9756       .9761         .9773       .9778       .9781       .9793       .9798       .9803       .9803       .9812         .9821       .9826       .9834       .9838       .9846       .9881       .9881         .9861       .9862       .9871       .9878       .9881       .9884       .9887         .9861       .9862       .9971       .9904       .9906       .9909       .9911       .9913         .9918       .9940       .9941       .9942       .9946       .9946       .9948       .9949       .9941         .9918       .9940       .9941       .9943       .9946       .9946       .9946       .9946       .9946       .9946         .9953       .9956       .9957       .9959       .9960       .9961       .9962       .9961       .9961       .9961       .9971       .9973       .9973       .9973       .9973       .9973       .9986       .9986       .9986       .9986       .9970       .9971	.9641       .9649       .9656       .9671       .9678       .9686       .9693       .9700         .9713       .9719       .9726       .9732       .9738       .9744       .9750       .9756       .9761         .9773       .9718       .9781       .9732       .9793       .9798       .9803       .9808       .9761         .9821       .9826       .9830       .9834       .9818       .9842       .9846       .9881       .9884       .9881         .9861       .9864       .9871       .9878       .9878       .9884       .9884       .9881         .9861       .9864       .9878       .9878       .9884       .9884       .9881         .9861       .9862       .9901       .9904       .9906       .9911       .9913       .9913         .9918       .9920       .9927       .9929       .9946       .9941       .9941       .9941         .9953       .9956       .9957       .9950       .9960       .9961       .9961       .9961         .9954       .9956       .9969       .9970       .9971       .9971       .9971         .9974       .9977       .9978       .9979       .9986 <t< td=""><td>1.7</td><td>.9554</td><td>.9564</td><td>.9573</td><td>.9582</td><td>1656</td><td>9599</td><td>9096</td><td>9196</td><td>.9625</td><td>.963</td></t<>	1.7	.9554	.9564	.9573	.9582	1656	9599	9096	9196	.9625	.963
.9713       .9716       .9726       .9732       .9738       .9744       .9750       .9756       .9761         .9773       .9718       .9781       .9782       .9793       .9798       .9803       .9808       .9717         .9821       .9826       .9830       .9834       .9838       .9846       .9850       .9881         .9861       .9826       .9831       .9838       .9846       .9881       .9884       .9884         .9861       .9862       .9901       .9904       .9906       .9906       .9911       .9913       .9913         .9918       .9920       .9921       .9927       .9929       .9946       .9948       .9949       .9931         .9918       .9940       .9941       .9943       .9946       .9946       .9948       .9949       .9941         .9953       .9956       .9957       .9959       .9960       .9961       .9962       .9963         .9954       .9956       .9957       .9957       .9978       .9979       .9971       .9971         .9941       .9942       .9984       .9984       .9984       .9986       .9989       .9969       .9969       .9969       .9969	.9713 .9719 .9726 .9732 .9738 .9744 .9750 .9756 .9761 .9773 .9778 .9783 .9788 .9783 .9789 .9803 .9808 .9812 .9821 .9826 .9830 .9834 .9838 .9842 .9846 .9850 .9854 .9881 .9864 .9868 .9871 .9878 .9878 .9881 .9884 .9887 .9891 .9901 .9904 .9906 .9909 .9911 .9913 .9918 .9920 .9922 .9925 .9927 .9929 .9911 .9913 .9938 .9940 .9941 .9943 .9946 .9948 .9949 .9951 .9953 .9955 .9956 .9957 .9959 .9960 .9951 .9958 .9956 .9967 .9968 .9969 .9970 .9971 .9973 .9974 .9977 .9978 .9984 .9988 .9989 .9989 .9989 .9989 .9989 .9989 .9988 .9988 .9988 .9988 .9988 .9988 .9988 .9988	89	.9641	9649	9656	.9664	1296.	8296.	9896	.9693	.9700	976.
.9773       .9778       .9783       .9783       .9793       .9798       .9803       .9808       .9812         .9821       .9826       .9830       .9834       .9836       .9846       .9850       .9854         .9861       .9864       .9868       .9871       .9878       .9846       .9850       .9854         .9861       .9864       .9871       .9878       .9881       .9884       .9887         .9893       .9896       .9901       .9904       .9906       .9909       .9911       .9913         .9918       .9940       .9941       .9943       .9946       .9948       .9949       .9941         .9953       .9956       .9957       .9959       .9960       .9961       .9962       .9961         .9957       .9957       .9959       .9960       .9961       .9962       .9963         .9978       .9978       .9979       .9979       .9979       .9979         .9981       .9982       .9984       .9984       .9986       .9986       .9986	.9773       .9778       .9783       .9783       .9793       .9798       .9803       .9808       .9812         .9821       .9826       .9830       .9834       .9838       .9846       .9850       .9854         .9861       .9864       .9836       .9871       .9878       .9846       .9850       .9857         .9861       .9864       .9878       .9878       .9881       .9884       .9881         .9893       .9866       .9901       .9904       .9906       .9901       .9911       .9913         .9918       .9920       .9927       .9927       .9929       .9946       .9941       .9941       .9941         .9953       .9956       .9957       .9959       .9960       .9961       .9963       .9961       .9963       .9961       .9961       .9963       .9961       .9961       .9961       .9963       .9961	6:1	.9713	.9719	.9726	.9732	.9738	.9744	.9750	.9756	1926.	.976
.9821     .9826     .9830     .9834     .9838     .9842     .9846     .9850     .9854       .9861     .9864     .9868     .9871     .9878     .9881     .9884     .9887       .9861     .9864     .9868     .9971     .9978     .9881     .9884     .9887       .9893     .9896     .9901     .9909     .9911     .9913       .9918     .9922     .9925     .9927     .9929     .9946     .9931     .9913       .9918     .9940     .9941     .9945     .9946     .9948     .9949     .9941       .9953     .9956     .9957     .9959     .9960     .9961     .9962     .9963       .9964     .9948     .9970     .9971     .9971     .9971       .9974     .9912     .9978     .9979     .9979       .9981     .9984     .9984     .9986     .9986	.9821       .9826       .9830       .9834       .9838       .9845       .9846       .9850       .9854         .9861       .9864       .9868       .9871       .9878       .9881       .9884       .9881         .9861       .9864       .9868       .9871       .9878       .9881       .9884       .9881         .9893       .9896       .9901       .9904       .9909       .9911       .9913         .9918       .9922       .9925       .9927       .9929       .9931       .9912       .9934         .9938       .9940       .9948       .9948       .9948       .9949       .9943       .9941         .9953       .9956       .9959       .9960       .9961       .9963       .9963       .9961       .9963       .9971       .9971       .9971       .9971       .9971       .9971       .9971       .9971       .9972       .9980       .9984       .9984       .9984       .9986       .9986       .9986       .9986       .9987       .9986       .9986       .9986       .9987       .9986       .9986       .9987       .9986       .9986       .9986       .9986       .9987       .9988       .9988       .9988       .9988	2.0	.9773	8776.	.9783	9788	.9793	.9798	.9803	9808	.9812	.9817
.9861       .9864       .9868       .9871       .9878       .9881       .9884       .9887         .9893       .9896       .9898       .9901       .9904       .9906       .9909       .9911       .9913         .9918       .9920       .9922       .9925       .9927       .9929       .9911       .9913       .9913         .9918       .9940       .9941       .9943       .9945       .9946       .9949       .9949       .9934         .9953       .9956       .9957       .9959       .9960       .9961       .9962       .9963         .9965       .9967       .9968       .9969       .9970       .9971       .9973         .9974       .9918       .9984       .9984       .9984       .9989       .9989	. 9861 . 9864 . 9868 . 9871 . 9878 . 9878 . 9881 . 9884 . 9887 . 9893 . 9896 . 9909 . 9911 . 9913 . 9918 . 9922 . 9922 . 9924 . 9906 . 9909 . 9911 . 9913 . 9918 . 9922 . 9925 . 9927 . 9929 . 9931 . 9932 . 9934 . 9935 . 9946 . 9948 . 9948 . 9949 . 9951 . 9953 . 9956 . 9956 . 9957 . 9959 . 9960 . 9961 . 9957 . 9965 . 9967 . 9968 . 9977 . 9977 . 9978 . 9978 . 9978 . 9988 . 9988 . 9988 . 9988 . 9988 . 9988 . 9988 . 9988	2.1	.9821	.9826	.9830	.9834	.9838	.9842	.9846	.9850	.9854	.9857
.9893       .9896       .9901       .9904       .9906       .9909       .9911       .9913         .9918       .9920       .9922       .9927       .9927       .9929       .9931       .9932       .9934         .9938       .9940       .9941       .9943       .9945       .9946       .9948       .9949       .9951         .9953       .9956       .9957       .9959       .9960       .9961       .9962       .9963         .9946       .9948       .9970       .9971       .9972       .9973         .9974       .9976       .9978       .9978       .9979       .9980         .9981       .9984       .9984       .9984       .9985       .9986       .9986	.9918 .9926 .9991 .9904 .9906 .9909 .9911 .9913 .9918 .9918 .9920 .9922 .9927 .9929 .9931 .9932 .9934 .9938 .9940 .9941 .9943 .9945 .9946 .9948 .9949 .9931 .9953 .9953 .9954 .9957 .9959 .9960 .9961 .9962 .9961 .9965 .9967 .9968 .9970 .9971 .9972 .9973 .9974 .9975 .9977 .9977 .9978 .9989 .9989 .9980 .9981 .9981 .9982 .9983 .9984 .9984 .9984 .9985 .9985 .9986	22	1986.	9864	9868	.9871	.9875	.9878	1886.	.9884	7886	986
.9918       .9920       .9925       .9927       .9929       .9931       .9932       .9934         .9938       .9940       .9941       .9943       .9946       .9946       .9948       .9949       .9951         .9953       .9956       .9957       .9959       .9960       .9961       .9962       .9963         .9957       .9968       .9969       .9970       .9971       .9971       .9971       .9971         .9974       .9978       .9977       .9978       .9979       .9980       .9984       .9984       .9984       .9985       .9986 </td <td>.9918 .9920 .9922 .9925 .9927 .9929 .9931 .9932 .9934 .9938 .9938 .9940 .9948 .9948 .9948 .9948 .9948 .9953 .9953 .9955 .9956 .9957 .9959 .9960 .9961 .9962 .9963 .9968 .9969 .9971 .9972 .9973 .9974 .9975 .9976 .9977 .9978 .9979 .9979 .9980 .9981 .9982 .9983 .9984 .9984 .9985 .9985 .9986</td> <td>2.3</td> <td>.9893</td> <td>9686</td> <td>9898</td> <td>1066.</td> <td>9904</td> <td>9066</td> <td>6066</td> <td>.9911</td> <td>.9913</td> <td>9916</td>	.9918 .9920 .9922 .9925 .9927 .9929 .9931 .9932 .9934 .9938 .9938 .9940 .9948 .9948 .9948 .9948 .9948 .9953 .9953 .9955 .9956 .9957 .9959 .9960 .9961 .9962 .9963 .9968 .9969 .9971 .9972 .9973 .9974 .9975 .9976 .9977 .9978 .9979 .9979 .9980 .9981 .9982 .9983 .9984 .9984 .9985 .9985 .9986	2.3	.9893	9686	9898	1066.	9904	9066	6066	.9911	.9913	9916
.9938 .9940 .9941 .9943 .9945 .9946 .9948 .9949 .9951 .9953 .9953 .9954 .9957 .9959 .9950 .9950 .9951 .9952 .9957 .9958 .9959 .9970 .9971 .9972 .9973 .9974 .9975 .9978 .9977 .9978 .9978 .9980 .9981 .9981 .9982 .9983 .9984 .9984 .9985 .9985 .9985	.9938 .9940 .9941 .9943 .9945 .9946 .9948 .9949 .9951 .9953 .9953 .9955 .9957 .9959 .9950 .9951 .9955 .9956 .9957 .9958 .9950 .9951 .9972 .9973 .9974 .9975 .9976 .9977 .9977 .9978 .9979 .9979 .9980 .9981 .9982 .9982 .9983 .9984 .9984 .9985 .9985 .9986	2.4	8166.	.9920	.9922	.9925	.9927	.9929	.9931	.9932	.9934	.993
. 9953 . 9955 . 9956 . 9957 . 9959 . 9960 . 9961 . 9962 . 9963 . 9965 . 9966 . 9967 . 9968 . 9969 . 9970 . 9971 . 9974 . 9976 . 9976 . 9977 . 9978 . 9989 . 9981 . 9981 . 9982 . 9983 . 9984 . 9984 . 9985 . 9985	. 9953 . 9955 . 9956 . 9957 . 9959 . 9960 . 9961 . 9962 . 9963 . 9965 . 9965 . 9968 . 9969 . 9970 . 9971 . 9972 . 9973 . 9974 . 9975 . 9976 . 9977 . 9978 . 9978 . 9979 . 9980 . 9981 . 9982 . 9983 . 9984 . 9984 . 9985 . 9986	2.5	.9938	.9940	.9941	.9943	.9945	.9946	.9948	.9949	1366.	.995
. 9965 . 9966 . 9967 . 9968 . 9969 . 9970 . 9971 . 9973 . 9973 . 9974 . 9975 . 9978 . 9978 . 9980 . 9980 . 9981 . 9982 . 9983 . 9984 . 9984 . 9985 . 9986	.9965 .9966 .9967 .9968 .9969 .9970 .9971 .9972 .9973 .9974 .9974 .9975 .9977 .9977 .9978 .9980 .9981 .9982 .9982 .9983 .9984 .9984 .9985 .9985	2.6	.9953	\$266.	9956	.9957	9989	0966	1966.	.9962	.9963	996.
. 9974 . 9975 . 9982 . 9983 . 9984 . 9988 .	.9974 .9975 .9976 .9977 .9978 .9978 .9980 .9980 .9980 .9981 .9981 .9982 .9983 .9984 .9984 .9985	2.7	.9965	9966	7966.	8966	6966	.9970	1766.	.9972	.9973	.997
9862, 9982, 9982, 9984, 9984, 9988, 9988, 9988	.9981 ,9982 ,9983 ,9984 ,9984 ,9985 ,9985 ,9986	2.8	.9974	5766.	9766.	7166.	7766.	8766	9766	9766.	.9980	.998
		2.9	1866:	.9982	.9982	.9983	.9984	.9984	.9985	\$866.	9866	.998

TABLE 9 Upper and Lower 90% and 80% Interval Values

FY	A.90up	A.901o	A.80up	A.801o	Regressed Norm. Flow
77	167.735	131.407	162.795	134.606	146.7
78	169.723	132.965	164.725	136.203	148.5
79	171.712	134.523	166.656	137.799	150.2
80	173.701	136.081	168.586	139.395	152.0
81	175.690	137.639	170.516	140.991	153.7
82	177.679	139.198	172.447	142.587	155.4
83	179.668	140.756	174.377	144.183	157.2
84	181.657	142.314	176.308	145.779	158.9
85	183.646	143.872	178.238	147.375	160.7

These examples are shown in Figure 7.

FIGURE 7 Upper and Lower 90% and 80% Interval Bands



Where: A = Actual Flow

B = Regressed Normalized Flow E = Upper 80% Interval

C = Upper 90% Interval

D = Lower 90% Interval

F = Lower 80% Interval

In order to produce a probabilistic forecast, selected interval or exceedence probability values can be calculated from a base forecast in a similar manner. However, the base forecast must have approximately the same meaning as the historic Normalized Flows; that is, the base forecast must be essentially a forecast of the historic normalized flow regression. In this case, equation 5 would be the appropriate forecast formula.

Actual Forecast Flow(p) = 
$$\frac{\text{Base Flow Forecast}}{\text{NFFadj} \pm \text{t(p)sNFFadj}}$$
 (5)

The following illustrative example of a forecast, with a 10% probability of exceedence, shows the slope of the Base Forecast increased to 2.0 mgd/yr beyond the historic data period where the slope of the Normalized Flow regression line was 1.74 mgd/yr.

Base Flow Forecast
Actual Forecast Flow(10%) = 
$$\frac{-----}{NFFadj}$$
 (6)

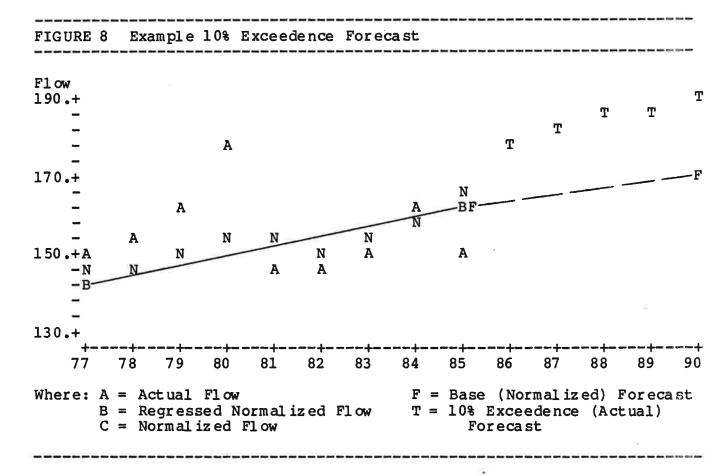
Where:

Base Flow Forecast (slope) = 
$$2.0 \text{ mgd/yr}$$
 (7)

The relevant data and results for this example are given in Table 10 and shown in Figure 7.

TABLE 10 Example 10% Exceedence Forecast Data

FY	Base Flow Forecast	Forecast Flow with 10% Prob. of Exceedence
86	162.7	180.5
87	164.7	182.7
88	166.7	185.0
89	168.7	187.2
90	170.7	189.4



Further elements of uncertainty can be incorporated into analysis and forecasting. These include probabilistic assignments to the future levels of other explanatory variables. For instance, if distribution functions are assigned to alternate scenarios of future population, housing units and employment, these could be combined with each other and those of the Normalized Flow Factors. The resulting forecast could be presented in terms of joint probabilities of exceedence based upon all the chosen explanatory variables.

### TASK 8

Ex-post examination of previous plans and forecasts for historical accuracy, bias and variance.

This Task, together with Task 1, most directly address the main issue of this study. A memo from Vice Chairman Jesse L. Maury to the other Commissioners and the General Manager dated October 17, 1984 discusses work load indices for FY '86 budget preparation. The primary subject of the memo concerns WSSC water production and sewage flow trends, and draws a comparison between Mr. Maury's extrapolation of short term historical trends and a forecast prepared by WSSC staff and reproduced in the report Flow Projections for Workload Indices by Mr. Bruce T. Downes dated November 7, 1984.

In the context of the results of this study, the forecasting methods employed by WSSC staff have greater merit.

The forecasts produced by WSSC staff are generally consistent with best contemporary practice; they are based upon unit use coefficients applied to disaggregated groups of customers (the forecasts of which have been estimated by independent agencies). The unit use coefficients (factors) are derived by WSSC staff in a very logical and conscientious manner. On the contrary, the straight line projections of past trends in raw data for total sewage flow and water production fall far short of good forecasts, given the fact that so much other relevant information is readily available.

In an attempt to reduce the computational burden, Mr. Maury (1984) constrained the intercept of his trend lines to the first data value in the time series of his analysis. This has the effect of skewing the slope (growth rate), which is the most important parameter value to be derived from the analysis. The same data produce the unconstrained slope values given in Table 11 for comparison.

Table 11	Analysis	Ωf	Trend	Slope	Data
TUDIC II	THICK TO TO	$\sim$ $_{\rm L}$	Trema	DIOPE	Data

767		Mr. Maury's Slope with Constrained Intercept	Slope with   Unconstrained   Intercept	Corr.
	Water Production	0.60 mgd/yr	1.33 mgd/yr	0.87
	Sewage Flows	0.14 mgd/yr	0.072 mgd/yr	0.03

Note: these analytical results are based on actual flows, not normalized flow.

Thus, the effect of constraining the intercept is to halve the growth rate for water production, and to double the growth rate for sewage flows. The savings in computational burden do not appear to be justified in the light of the relative magnitude of skew introduced into the results.

The following sewage flow and water production factors were used in the work described by Mr. Downes (1984):

	Sewage	Water,
	(gpd)	(gpd)
Single Family Dwelling Units	350	270
Multi-family Dwelling Units	330	253
Employment (Montgomery Co.)	49	60
(Prince George's Co.	.) 73	60

The source of information for numbers of dwelling units and employment figures is not made clear in the memo.

Sewage flows from 1972 to 1984, normalized for variations in annual rainfall, are represented by a regression line which shows an annual increase of 2.3 mgd. The forecasts just described used the normalized FY '84 flow as the base from which to start. A better base would have been the flow for FY '84 represented by the regression line; the implication being that it is the normalized flow which is being forecast, and that the regression line is its representation during the recent past. The 1984 base represented by the regression would be approximately 2.5 mgd lower than the normalized flow for FY '84, and thus each of the values in the forecast should be reduced by that amount.

The history of sewage flow factors used at WSSC is documented in the report The Development of Sewage Flow Factors and Their Use in Forecasting Sewage Flow by Edward Graham and dated November 1981. The description of WSSC sewage flow forecasts in that report is reproduced here for easy reference.

"Growth forecasts are provided by M-NCPPC, generally in 5-year increments, for population, dwelling units and employment. These can be prepared for appropriate sewer service areas. Accordingly, sewage flow forecasts can most easily be prepared using these data. The approach is quite straightforward:

1. Determine existing flow

Determine 'base' flow factors, based on water consumption, for employment and dwelling units,

- 3. Determine a composite flow factor to include an infiltration allowance.
- 4. Determine the flow increase from the growth projections and flow factors,
- 5. Prepare raw flow forecasts,
- 6. Adjust forecast as appropriate to reflect cost-effective I/I reduction.

This method has been expanded, and improved, to include normalization for annual rainfall in step 1. Present practice at WSSC also involves the use of only recently connected properties (assumed recently constructed) in order to determine "base" flow factors representative of the types of dwellings (plumbing systems and water using appliances) that will be contributing to future growth in sewage flow.

A recent analysis of residential sewage flow factors (Del Grosso and Downes, 1984) resulted in the recommendation that single family dwelling unit flow factors be reduced from 350 to 300 gpd and that those for multi-family units be reduced from 330 to 270 gpd.

One of the most significant changes in the way water and sewage flows are forecast is in the use of dwelling units as predictors instead of population. The analysis done on the subject at the time of the <u>Bi-County Water Supply Study</u> indicated that a better relationship existed between water use and dwellings than water use and population.

In general, water and sewage flow factors have been refined downward as analysis and data handling capabilities have improved. Concurrently, the high rates of growth experienced in earlier decades have not continued in the past few years and the ultimate carrying capacity of the land (development potential) has been increasingly taken into account as a limiting factor when long range forecasts are made.

Successive housing unit and employment forecasts produced by the counties and the Cooperative Forecasting Program have declined. All three future scenarios of the Round III dwelling unit forecast for Prince George's County lie below the intermediate scenario of Round II. All of the Round III employment scenarios lie below the lowest of Round II. The variance (spread) of employment scenarios is wider, whereas that of dwelling units is narrower in the more recent Round. Although the forecasts have not had long to run, it can be seen that the earlier ones were for future levels of development which would take longer to materialize than expected.

#### TASK 9

Outline future directions in data availability, analytical tools, forecasting techniques, and planning applications.

The detail and availability of data with respect to water production and sewer flows in the WSSD has improved dramatically in recent years. This is mostly due to the computerization of billing records and the generation of routine reports which classify the data in useful ways. It is expected that improvements will continue to be made in the way the data is stored, but the most important beneficial feature in the short term will be the increased access to this data directly by the different divisions of the Commission through the use of remote terminals and analytical tools such as the FOCUS software used for statistical analysis. The implementation of the Sewer System Computer Model should make spatial and temporal sewage flow data readily available on a very fine scale.

The cohort survival model made a great improvement in the field of population forecasting when it gained widespread acceptance. It was used in the Round II Cooperative Forecasts for Prince George's County, but because of the overwhelming influence of migration in recent years, it was not used in Round III. Other ways of using diverse data will be developed to forecast population where migration continues to dominate. Multiple regression analysis will gain in applications where the combined effects of multiple explanatory variables are desired to be segregated. The use of multiple regressions could also help in deriving factors for use in forecasting.

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Wolman, Abel, (see also Board of Engineers).

## Appendix

National Oceanic and Atmospheric Administration: example of Climatological Data

JANUARY 1981

VOLUME 85

NUMBER 1

# Climatological Data

MARYLAND AND DELAWARE

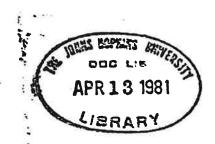


## TEMPERATURE AND PRECIPITATION EXTREMES

HIGHEST TEMPERATURE:	LA PLATA 1 H	MD.	62	DATE	26
LOHEST TEMPERATURE:	OAKLAND 1 SE	MD.	-14	DATE	09
GREATEST TOTAL PRECIPITATION:	MC HENRY 2 NH	MD.	1.78		
LEAST TOTAL PRECIPITATION:	HANCOCK FRUIT LAB	MD.	.20		
GREATEST 1 DAY PRECIPITATION:	HILMGTON PORTER RESVR	DEL.	.41	DATE	07
GREATEST TOTAL SNOHFALL:	OAKLAND 1 SE	MO.	28.5		
GREATEST DEPTH OF SNOW OR ICE:	FROSTBURG 2	MO.	13	DATE	18+

## SUPPLEMENTAL DATA

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I CERTIFY THAT THIS IS AN OFFICIAL PUBLICATION OF THE NATIONAL OCEANIC AND ATMOSPHERIC ADMINISTRATION AND IS COMPILED FROM RECORDS ON FILE AT THE NATIONAL CLIMATIC CENTER, ASHEVILLE, NORTH CAROLINA 2001.

Pariel B. Metallo DI NATIONAL CLIMATIC

NATIONAL OCEANIC AND ATMOSPHERIC ADMINISTRATION / ENVIRONMENTAL DATA AND / NATIONAL CLIMATIC CENTER ATMOSPHERIC ADMINISTRATION / INFORMATION SERVICE / ASHEVILLE, N.C.

## DAILY PRECIPITATION

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